

# The ChairX Math package

ChairX  
Version v1.0.0 (2021/07/29)  
`marvin.dippell@mathematik.uni-wuerzburg.com`

July 30, 2021

## **Abstract**

This is a part of the new ChairX package providing the famous ChairX macros for mathematics.

## Contents

|          |                                      |           |
|----------|--------------------------------------|-----------|
| <b>1</b> | <b>Introduction</b>                  | <b>2</b>  |
| <b>2</b> | <b>Usage</b>                         | <b>2</b>  |
| 2.1      | Fonts . . . . .                      | 2         |
| 2.2      | New Delimiters . . . . .             | 4         |
| 2.3      | General Mathematics Macros . . . . . | 5         |
| 2.4      | Algebra . . . . .                    | 7         |
| 2.5      | Analysis . . . . .                   | 10        |
| 2.6      | Category Theory . . . . .            | 13        |
| 2.7      | Differential Geometry . . . . .      | 14        |
| 2.8      | Linear Algebra . . . . .             | 18        |
| 2.9      | Statistics . . . . .                 | 19        |
| 2.10     | Topology . . . . .                   | 19        |
| <b>3</b> | <b>Implementation</b>                | <b>20</b> |
| 3.1      | Fonts . . . . .                      | 20        |
| 3.2      | New Delimiters . . . . .             | 24        |
| 3.3      | General Mathematics Macros . . . . . | 24        |
| 3.4      | Algebra . . . . .                    | 27        |
| 3.5      | Analysis . . . . .                   | 31        |
| 3.6      | Category Theory . . . . .            | 35        |
| 3.7      | Differential Geometry . . . . .      | 37        |
| 3.8      | Linear Algebra . . . . .             | 43        |
| 3.9      | Statistics . . . . .                 | 44        |
| 3.10     | Topology . . . . .                   | 45        |

# 1 Introduction

This package defines the new package `chairxmath`. It can be used as a standalone version of the math macros from `nchairx` if the other settings and defaults of `nchairx` are not needed or wanted.

## 2 Usage

### 2.1 Fonts

The package uses different fonts for different groups of macros. The font used for a particular macro is mentioned in the description of that macro. The groups of fonts are:

- **algebrafont** for generic algebras.  
Can be accessed via `\algebra`.  
Default font: `\mathscr`
- **basisfont** for bases of vector spaces.  
Can be accessed via `\basis`.  
Default font: `\mathit`
- **categoryfont** for generic categories.  
Can be accessed via `\category`.  
Default font: `\mathfrak`
- **categorynamefont** for predefined categories.  
Can be accessed via `\categoryname`.  
Default font: `\mathsf`
- **fieldfont** for generic fields.  
Can be accessed via `\field`.  
Default font: `\mathbb`
- **filterfont** for generic filters.  
Can be accessed via `\filter`.  
Default font: `\mathfrak`
- **functorfont** for generic functors.  
Can be accessed via `\functor`.  
Default font: `\mathsf`
- **gerstenhaberfont** for generic Gerstenhaber algebras.  
Can be accessed via `\gerstenhaber`.  
Default font: `\mathfrak`
- **groupfont** for the matrix groups.  
Can be accessed via `\group`.  
Default font: `\mathrm`

- **groupoidfont** for generic groupoids.  
Can be accessed via `\groupoid`.  
Default font: `\mathfrak`
- **hilbertfont** for Hilbert spaces.  
Can be accessed via `\hilbert`.  
Default font: `\mathfrak`
- **liealgfont** for generic Lie algebras.  
Can be accessed via `\liealg`.  
Default font: `\mathfrak`
- **modulefont** for generic modules.  
Can be accessed via `\module`.  
Default font: `\mathscr`
- **prehilbfont** for pre-Hilbert space.  
Can be accessed via `\prehilb`.  
Default font: `\mathcal`
- **operatorfont** for most common operators.  
Can be accessed via `\operator`.  
Default font: `\mathrm`
- **ringfont** for generic rings.  
Can be accessed via `\ring`.  
Default font: `\mathsf`
- **scriptfont** for subscripts.  
Can be accessed via `\script`.  
Default font: `\mathrm`
- **sheaffont** for generic sheaves.  
Can be accessed via `\sheaf`.  
Default font: `\mathscr`
- **spacesfont** for predefined function spaces, e.g. `\Bounded`  
Default font: `\mathscr`
- **topologyfont** for generic topologies.  
Can be accessed via `\topology`  
Default font: `\mathscr`

`\chairxfonts` The `\chairxfonts` macro can be used to redefine the fonts of the different groups of macros. It takes as argument a comma separated list of group names and the new font macros, e.g.

```
\chairxfonts{algebrafont = \mathfrak, scriptfont = \mathrm}
```

## 2.2 New Delimiters

We use `\DeclarePairedDelimiters` to generate all kind of bracket expressions of variable size as used e.g. in differential geometry. This has the big advantage that one has two options to set the size of the brackets: either with an explicit optional argument `\big`, ..., `\Bigg`, `\vast`, or `\Vast` like

$$\text{\Schouten}[\vast]{X, Y}: \left[ \begin{array}{c} X, Y \\ \end{array} \right]_s$$

or you can use the \*-version which produces automatic sizes via `\left` and `\right`.

$$\text{\abs*{\lim\limits_{n\rightarrow\infty} b_n}} \text{ yields } \left| \lim_{n \rightarrow \infty} b_n \right|$$

Note, however, that this will typically result in sub-optimal spacing. Also, the brackets turn out to be typically too large.

Note that using the bracket constructions with `\DeclarePairedDelimiters` gives typically much better spacing than doing things by hand:

$$\text{good } \text{\abs{\det(A)}}: |\det(A)| \quad \text{bad } |\det(A)|: |\det(A)|$$

- `\vast` In many formulas one needs large delimiters typically ranging from `\big` to `\Bigg`.
- `\Vast` However, in very large formula constructions even that is not enough. To have a systematic enlargement the following delimiters sizes are introduced: `\vast` and `\Vast` together with the corresponding helper macros `\vastl`, `\vastr`, `\vastm`, `\vastl`, `\Vastr`, and `\Vastm` needed to define pairs of delimiters. They allow to produce large (pairs of) delimiters, always provided that the corresponding font has the symbols in the correct size.
- `\Vastr` The following commands allow for an option size argument:

- Absolute value `\abs`
- Generic norm `\norm`
- Supremum norm `\supnorm`
- Essential supremum norm `\essupnorm`
- Dirac ket `\ket`
- Dirac bra `\bra`
- Dirac ketbra `\ketbra`
- Dirac braket `\braket`
- Schouten bracket `\Schouten`
- Nijenhuis-Richardson bracket `\NRbracket`

- Frölicher-Nijenhuis bracket `\FNbracket`
- Courant bracket `\Courant`
- Dorfman bracket `\Dorfman`
- Generic scalar product `\SP`
- Generic inner product with decorations `\IP`
- Restriction of a map `\at`
- Étale space of a presheaf `\etale`

## 2.3 General Mathematics Macros

### 2.3.1 General Math Commands

|                         |   |
|-------------------------|---|
| <code>\I</code>         | Imaginary unit <code>\I: i</code>   |
| <code>\E</code>         | Euler number <code>\E: e</code>   |
| <code>\D</code>         | Differential <code>\D x: dx</code>  |
| <code>\cc</code>        | Complex conjugation <code>z \mapsto \cc{z}: z \mapsto \bar{z}</code>  |
| <code>\sign</code>      | Signum <code>\sign \sigma: sign \sigma</code><br>Uses <code>operatorfont</code> .                             |
| <code>\RE</code>        | Real part (the standard symbols are sooo ugly) <code>\RE(z): Re(z)</code><br>Uses <code>operatorfont</code> . |
| <code>\IM</code>        | Imaginary part <code>\IM(z): Im(z)</code><br>Uses <code>operatorfont</code> .                                 |
| <code>\Unit</code>      | Unit element <code>\Unit: \mathbb{1}</code>   |
| <code>\const</code>     | Generic constant <code>\const: const</code><br>Uses <code>mathit</code> as font.                              |
| <code>\canonical</code> | Subscript for canonical <code>\omega_\canonical: \omega_{\text{can}}</code><br>Uses <code>scriptfont</code> . |
| <code>\pt</code>        | A single point <code>\{\pt\}: \{pt\}</code><br>Uses <code>operatorfont</code>                                 |

### 2.3.2 Restrictions

|                  |   |
|------------------|---|
| <code>\at</code> | Restriction of a map to a subset <code>f \at{U}: f _U</code> or with optional size <code>f \at[\Big]{U}: f _U</code> .<br>Default size is <code>\big</code> . |
|------------------|---|

### 2.3.3 Maps and Related Stuff

|                   |  |
|-------------------|--|
| <code>\Map</code> | Space of maps <code>\Map(X, Y): Map(X, Y)</code><br>Uses <code>operatorfont</code> .       |
| <code>\Bij</code> | Space of bijections <code>\Bij(X, Y): Bij(X, Y)</code><br>Uses <code>operatorfont</code> . |

|                        |   |
|------------------------|---|
| <code>\argument</code> | Generic argument of a map $f(\text{\argument})$ : $f(\cdot)$  |
| <code>\domain</code>   | Domain of a map $\text{\domain}(\phi)$ : $\text{dom}(\phi)$<br>Uses <code>operatorfont</code> .   |
| <code>\range</code>    | Range of a map $\text{\range}(\phi)$ : $\text{range}(\phi)$<br>Uses <code>operatorfont</code> .   |
| <code>\id</code>       | Identity map $\text{\id}$ : $\text{id}$<br>Uses <code>operatorfont</code> .   |
| <code>\pr</code>       | Generic projection $\text{\pr} \text{\colon} E \rightarrow M$ : $E \rightarrow M$<br>Uses <code>operatorfont</code> .   |
| <code>\inv</code>      | Inversion map $\text{\inv} \text{\colon} g \mapsto g^{-1}$ : $\text{inv}: g \mapsto g^{-1}$<br>Uses <code>operatorfont</code> .   |
| <code>\ev</code>       | Evaluation map $\text{\ev} \text{\colon} V \otimes V^* \rightarrow \mathbb{k}$ : $\text{ev}: V \otimes V^* \rightarrow \mathbb{k}$<br>Uses <code>operatorfont</code> .  |
| <code>\image</code>    | Image of a map $\text{\image}(f)$ : $\text{im}(f)$<br>Uses <code>operatorfont</code> .  |
| <code>\graph</code>    | Graph of a map $\text{\graph}(f)$ : $\text{graph}(f)$<br>Uses <code>operatorfont</code> .   |
| <code>\coimage</code>  | Coimage of a map $\text{\coimage}(f)$ : $\text{coim}(f)$<br>Uses <code>operatorfont</code> .  |
| <code>\coker</code>    | Cokernel of a map $\text{\coker}(f)$ : $\text{coker}(f)$<br>Uses <code>operatorfont</code> .  |
| <code>\operator</code> | This macro allows to construct own mathematical operators whose fonts are consistent with the predefined operators of <code>nchairs</code> $\text{\operator}\{asso\}$ : $\text{asso}$<br>Uses <code>operatorfont</code> . |

### 2.3.4 Relations

|                       |  |
|-----------------------|--|
| <code>\later</code>   | Later in a directed set $i \text{\later} j$ : $i \succ j$            |
| <code>\earlier</code> | Earlier in a directed set $i \text{\earlier} j$ : $i \preccurlyeq j$ |

### 2.3.5 Big Sums and Products

|                       |  |
|-----------------------|--|
| <code>\bigplus</code> | A big plus sign that can be decorated with limits. Similar to the usual sum it can be used inline $\text{\bigplus}_{k=1}^n V_k$ and in <code>displaystyle</code> : |
|-----------------------|--|

$$\sum_{k=1}^n V_k$$

|                        |  |
|------------------------|--|
| <code>\bigtimes</code> | A big times sign that can be decorated with limits. Similar to the usual sum it can be used inline $\text{\bigtimes}_{k=1}^n V_k$ and in <code>displaystyle</code> : |
|------------------------|--|

$$\bigotimes_{k=1}^n V_k$$

|                      |   |
|----------------------|---|
| <code>\biprod</code> | A biproduct sign that can be decorated with limits. Similar to the usual sum it |
|----------------------|---|

can be used inline `\biprod_{k=1}^n V_k`:  $\prod_{k=1}^n V_k$  and in `displaystyle`:

$$\prod_{k=1}^n V_k$$

### 2.3.6 Labels

In proofs we sometimes want to label an equation by a symbol and not by an equation number. Typical choices are of course `(*)` or `(**)`. But as proofs become longer, some additional labels are nice to have:

|                       |                              |
|-----------------------|------------------------------|
| <code>\smiley</code>  | A smiley $\smiley \odot$     |
| <code>\frownie</code> | A frownie $\frownie \ominus$ |
| <code>\heart</code>   | A heart $\heart \heartsuit$  |

## 2.4 Algebra

### 2.4.1 Fonts for Rings and Things

|                            |   |
|----------------------------|---|
| <code>\field</code>        | Font for rings <code>\field{R}</code> : $\mathbb{R}$<br>Uses <code>fieldfont</code> .   |
| <code>\ring</code>         | Font for rings <code>\ring{C}</code> : $C$<br>Uses <code>ringfont</code> .  |
| <code>\group</code>        | Font for particular (matrix) groups <code>\group{SO}(3)</code> : $SO(3)$<br>Uses <code>groupfont</code> .   |
| <code>\algebra</code>      | Font for algebras <code>\algebra{A}</code> : $\mathcal{A}$<br>Uses <code>algebrafont</code> .   |
| <code>\module</code>       | Font for modules <code>\module{M}</code> : $\mathcal{M}$<br>Uses <code>modulefont</code> .  |
| <code>\liealg</code>       | Font for Lie algebras <code>\liealg{g}</code> : $\mathfrak{g}$<br>Uses <code>liealgfont</code> .  |
| <code>\MC</code>           | MC for Maurer-Cartan as a tiny index <code>\mu_\MC \in \liealg{g}^1</code> : $\mu_{\mathcal{M}} \in \mathfrak{g}^1$<br>Uses <code>scriptfont</code> . |
| <code>\gerstenhaber</code> | Font for Gerstenhaber algebras <code>\gerstenhaber{G}</code> : $\mathfrak{G}$<br>Uses <code>gerstenhaberfont</code> .                                 |

### 2.4.2 Some Symbols needed in Algebra

|                     |  |
|---------------------|--|
| <code>\Pol</code>   | Polynomials and polynomial functions <code>\Pol(T^*Q)</code> : $Pol(T^*Q)$<br>Uses <code>operatorfont</code> . |
| <code>\lmult</code> | Left multiplications <code>\lmult_a</code> : $\ell_a$<br>Uses <code>operatorfont</code> .                      |
| <code>\rmult</code> | Right multiplications <code>\rmult_b</code> : $r_b$<br>Uses <code>operatorfont</code> .                        |
| <code>\Lmult</code> | Left multiplications <code>\Lmult_a</code> : $L_a$<br>Uses <code>operatorfont</code> .                         |
| <code>\Rmult</code> | Right multiplications <code>\Rmult_b</code> : $R_b$  |

|            |  |
|------------|--|
|            | Uses <code>operatorfont</code> .   |
| \Center    | Center \Center(\code{A}): $\mathcal{L}(\mathcal{A})$   |
| \ad        | Adjoint action (infinitesimal) \ad(a): $\text{ad}(a)$<br>Uses <code>operatorfont</code> .  |
| \Ad        | Adjoint action \Ad_g: $\text{Ad}_g$<br>Uses <code>operatorfont</code> .  |
| \Conj      | Conjugation \Conj_g: $\text{Conj}_g$<br>Uses <code>operatorfont</code> .   |
| \acts      | A generic (left) action map g \acts a: $g \triangleright a$  |
| \racts     | A generic right action map a \racts g: $a \triangleleft g$   |
| \Char      | Characteristics of a field \Char(\mathbb{k}): $\text{char}(\mathbb{k})$<br>Uses <code>operatorfont</code> .  |
| \modulo    | Yet another modulo n \modulo 2: $n \bmod 2$<br>Uses <code>operatorfont</code> .  |
| \Clifford  | Clifford algebra generated by a vector space and a bilinear form: \Clifford(V, h): $\text{Cl}(V, h)$<br>Uses <code>operatorfont</code> .                             |
| \cClifford | Complex Clifford algebra \cClifford(V, h): $\mathbb{C}\text{Cl}(V, h)$<br>Uses <code>operatorfont</code> .   |
| \Der       | (*-Derivations \Der(\code{A}): $\text{Der}(\mathcal{A})$<br>\Der*(\code{A}): ${}^*\text{-Der}(\mathcal{A})$<br>Uses <code>operatorfont</code> .                      |
| \InnDer    | Inner (*-)derivations \InnDer(\code{A}): $\text{InnDer}(\mathcal{A})$<br>\InnDer*(\code{A}): ${}^*\text{-InnDer}(\mathcal{A})$<br>Uses <code>operatorfont</code> .   |
| \OutDer    | Outer (*-)derivations \OutDer(\code{A}): $\text{OutDer}(\mathcal{A})$<br>\OutDer*(\code{A}): ${}^*\text{-OutDer}(\mathcal{A})$<br>Uses <code>operatorfont</code> .   |
| \InnAut    | Inner (*-)automorphisms \InnAut(\code{A}): $\text{InnAut}(\mathcal{A})$<br>\InnAut*(\code{A}): ${}^*\text{-InnAut}(\mathcal{A})$<br>Uses <code>operatorfont</code> . |
| \OutAut    | Outer (*-)automorphisms \OutAut(\code{A}): $\text{OutAut}(\mathcal{A})$<br>\OutAut*(\code{A}): ${}^*\text{-OutAut}(\mathcal{A})$<br>Uses <code>operatorfont</code> . |
| \formal    | Formal power series in some variables V\formal{\lambda}: $V[[\lambda]]$  |
| \laurent   | Formal Laurent series in some variables V\laurent{\lambda}: $V((\lambda))$   |
| \sweedler  | Smaller index for Sweedler notation in Hopf algebra theory<br>\Delta(a) = a_\sweedler{1} \tensor a_\sweedler{2}: $\Delta(a) = a_{(1)} \otimes a_{(2)}$               |

### 2.4.3 Categories from Algebra

|           |   |
|-----------|---|
| \algebras | Category of algebras \algebras: <code>alg</code><br>Category of *-algebras \algebras*: <code>*-alg</code><br>Uses <code>categorynamefont</code> . |
| \Algebras | Category of unital algebras \Algebras: <code>Alg</code>   |

|               |  |
|---------------|--|
|               | Category of unital $*$ -algebras \Algebras*: $^*-\text{Alg}$<br>Uses <code>categorynamefont</code> .   |
| \reps         | Category of $(*)$ -representations \reps_\algebra{C}(\algebra{B}): $\text{rep}_{\mathcal{C}}(\mathcal{B})$<br>\reps*_\algebra{C}(\algebra{B}): $^*-\text{rep}_{\mathcal{C}}(\mathcal{B})$<br>Uses <code>categorynamefont</code> .                          |
| \Reps         | Category of strongly non-degenerate $(*)$ -representations \Reps_\algebra{A}(\algebra{B}): $\text{Rep}_{\mathcal{A}}(\mathcal{B})$<br>\Reps*_\algebra{A}(\algebra{B}): $^*-\text{Rep}_{\mathcal{A}}(\mathcal{B})$<br>Uses <code>categorynamefont</code> .  |
| \PoissonAlg   | Category of $(*)$ -Poisson algebras \PoissonAlg: PoissonAlg<br>\PoissonAlg*: $^*-\text{PoissonAlg}$<br>Uses <code>categorynamefont</code> .  |
| \modules      | Category of (inner product) modules \modules_\algebra{A}(\algebra{B}):<br>mod_{\mathcal{A}}(\mathcal{B})<br>\modules*_\algebra{A}(\algebra{B}): $^*-\text{mod}_{\mathcal{A}}(\mathcal{B})$<br>Uses <code>categorynamefont</code> .                         |
| \Leftmodules  | Category of left modules \Leftmodules{\algebra{A}}: $\mathcal{A}\text{-mod}$<br>Uses <code>categorynamefont</code> .   |
| \Rightmodules | Category of right modules with optional subscript \Rightmodules[\category{C}]{\algebra{A}}:<br>mod_{\mathcal{C}-\mathcal{A}}   |
| \Modules      | Category of strongly non-degenerate (inner product) modules \Modules_\algebra{A}(\algebra{B}):<br>Mod_{\mathcal{A}}(\mathcal{B})<br>\Modules*_\algebra{A}(\algebra{B}): $^*-\text{Mod}_{\mathcal{A}}(\mathcal{B})$<br>Uses <code>categorynamefont</code> . |
| \LeftModules  | Category of strongly non-degenerate left modules \LeftModules{\algebra{A}}:<br>$\mathcal{A}\text{-Mod}$<br>Uses <code>categorynamefont</code> .  |
| \RightModules | Category of strongly non-degenerate right modules with optional subscript<br>\RightModules{\algebra{A}}: Mod- $\mathcal{A}$ or \RightModules[\category{C}]{\algebra{A}}:<br>Mod_{\mathcal{C}-\mathcal{A}}  |
| \Bimodules    | Category of (inner product) bimodules \Bimodules(\algebra{A},\algebra{B}):<br>Bimod(\mathcal{A},\mathcal{B})<br>\Bimodules*(\algebra{A},\algebra{B}): $^*-\text{Bimod}(\mathcal{A},\mathcal{B})$<br>Uses <code>categorynamefont</code> .                   |
| \Rings        | Category of unital rings (meant to be associative) \Rings: Ring<br>Uses <code>categorynamefont</code> .  |
| \Groups       | Category of groups \Groups: Group<br>Uses <code>categorynamefont</code> .  |
| \Ab           | Category of abelian groups \Ab: Ab<br>Uses <code>categorynamefont</code> .   |
| \Lattices     | Category of lattices \Lattices: Lattice<br>Uses <code>categorynamefont</code> .  |
| \Sets         | Category of sets \Sets: Set<br>Uses <code>categorynamefont</code> .  |
| \Vect         | Category of vector spaces \Vect: Vect  |

|            |  |
|------------|--|
|            | Uses <code>categorynamefont</code> .   |
| \LieAlgs   | Category of Lie algebras \LieAlgs: LieAlg<br>Uses <code>categorynamefont</code> .                      |
| \Posets    | Category of partially ordered sets \Posets: Poset<br>Uses <code>categorynamefont</code> .              |
| \Directed  | Category of directed sets \Directed: Directed<br>Uses <code>categorynamefont</code> .                  |
| \GSets     | Category of $G$ -Sets \GSets: $G$ -Set and \Gsets[H]: $H$ -Set<br>Uses <code>categorynamefont</code> . |
| \Groupoids | Category of groupoids \Groupoids: Groupoid<br>Uses <code>categorynamefont</code> .                     |

## 2.5 Analysis

### 2.5.1 General Anyalsis Macros

|           |   |
|-----------|---|
| \vol      | Volume \vol: vol<br>Uses <code>operatorfont</code>  |
| \complete | Completion of some space \complete{v}: $\widehat{V}$  |
| \Ball     | Open ball \Ball_{r}(p): $B_r(p)$  |
| \abs      | Generic absolute value \abs{x}: $ x $   |
| \norm     | Generic norm \norm{v}: $\ v\ $  |
| \supnorm  | Supremum norm \supnorm{f}: $\ f\ _\infty$   |
| \expands  | Formal expansions $f(t) \stackrel{\text{stackrel}}{\longrightarrow} 0$ \expands t^k: $f(t) \xrightarrow{t \rightarrow 0} t^k$ ,<br>or with optional stretching factor (default is 2.5) a \expands[4] b: $a \xrightarrow{\text{expands}[4]} b$ . |

### 2.5.2 Pseudodifferential Operators

|         |   |
|---------|---|
| \std    | Standard ordering as small subscript \sigma_\std: $\sigma_{\text{std}}$<br>Uses <code>scriptfont</code>         |
| \Weyl   | Weyl ordering as small subscript \sigma_\Weyl: $\sigma_{\text{Weyl}}$<br>Uses <code>scriptfont</code>           |
| \Op     | Operator for a symbol \Op(f): $\text{Op}(f)$<br>Uses <code>operatorfont</code>                                  |
| \Opstd  | Standard ordered operator for a symbol \Opstd(f): $\text{Op}_{\text{std}}(f)$<br>Uses <code>operatorfont</code> |
| \OpWeyl | Weyl ordered operator for a symbol \OpWeyl(f): $\text{Op}_{\text{Weyl}}(f)$<br>Uses <code>operatorfont</code>   |

### 2.5.3 Function Spaces

|             |   |
|-------------|---|
| \spacename  | Font for specific functional spaces \spacename{F}(X): $\mathcal{F}(X)$<br>Uses <code>spacefont</code> . |
| \Bounded    | Bounded functions \Bounded(X): $\mathcal{B}(X)$<br>Uses <code>spacefont</code> .                        |
| \Continuous | Continuous functions \Continuous(X): $\mathcal{C}(X)$   |

|                               |  |
|-------------------------------|--|
| <code>\Contbound</code>       | Uses <code>spacefont</code> .<br>Continuous bounded functions $\text{\Contbound}(X)$ : $\mathcal{C}_b(X)$  |
| <code>\Fun</code>             | Uses <code>spacefont</code> .<br>$C^k$ -functions (for $\mathcal{C}$ use <code>\Continuous</code> ) $\text{\Fun}(M)$ : $\mathcal{C}^k(M)$ and $\text{\Fun}[\text{\ell}] (M)$ : $\mathcal{C}^\ell(M)$ |
| <code>\Cinfty</code>          | Uses <code>spacefont</code> .<br>Smooth functions $\text{\Cinfty}$ : $\mathcal{C}^\infty(M)$   |
| <code>\Comega</code>          | Uses <code>spacefont</code> .<br>Real-analytic functions $\text{\Comega}$ : $\mathcal{C}^\omega(M)$  |
| <code>\Holomorphic</code>     | Uses <code>spacefont</code> .<br>Holomorphic functions $\text{\Holomorphic}$ : $\mathcal{O}(U)$  |
| <code>\AntiHolomorphic</code> | Uses <code>spacefont</code> .<br>Anti-holomorphic functions $\text{\AntiHolomorphic}$ : $\overline{\mathcal{O}}(U)$  |
| <code>\Schwartz</code>        | Uses <code>spacefont</code> .<br>Schwartz space $\text{\Schwartz}$ : $\mathcal{S}(\mathbb{R}^n)$   |
| <code>\Riemann</code>         | Uses <code>spacefont</code> .<br>Riemann integrable functions $\text{\Riemann}([a, b])$ : $\mathcal{R}([a, b])$  |

#### 2.5.4 Locally Convex Analysis and Distributions

|                         |   |
|-------------------------|---|
| <code>\sing supp</code> | Singular support of a distribution $\text{\sing supp } u$ : $\text{sing supp } u$ |
| <code>\seminorm</code>  | Font for generic seminorm $\text{\seminorm}\{p\}$ : $p$                           |
| <code>\ord</code>       | Order of a distribution $\text{\ord}(u)$ : $\text{ord}(u)$                        |
| <code>\conv</code>      | Convex hull $\text{\conv}(A)$ : $\text{conv}(A)$                                  |
| <code>\extreme</code>   | Extreme points $\text{\extreme}(A)$ : $\text{extreme}(A)$                         |

#### 2.5.5 Hilbert Spaces and Operators

|                           |  |
|---------------------------|--|
| <code>\hilbert</code>     | Font for Hilbert spaces $\text{\hilbert}\{H\}$ : $\mathfrak{H}$<br>Uses <code>hilbertfont</code>   |
| <code>\prehilb</code>     | Font for pre-Hilbert spaces $\text{\prehilb}\{H\}$ : $\mathcal{H}$<br>Uses <code>prehilbfont</code> .  |
| <code>\Adjointable</code> | Adjointable operators $\text{\Adjointable}(\text{\hilbert}\{H\})$ : $\mathfrak{B}(\mathfrak{H})$ or with optional argument $\text{\Adjointable}[\text{\algebra}\{A\}](\text{\hilbert}\{H\})$ : $\mathfrak{B}_{\mathcal{A}}(\mathfrak{H})$ if we have a Hilbert module over an algebra $\mathcal{A}$ instead. |
| <code>\Finite</code>      | Finite rank operators $\text{\Finite}(\text{\hilbert}\{H\})$ : $\mathfrak{F}(\mathfrak{H})$ or with optional argument $\text{\Finite}[\text{\algebra}\{A\}](\text{\module}\{H\})$ : $\mathfrak{F}_{\mathcal{A}}(\mathcal{H})$  |
| <code>\Compact</code>     | Compact operators $\text{\Compact}(\text{\hilbert}\{H\})$ : $\mathfrak{K}(\mathfrak{H})$ or with optional argument $\text{\Compact}[\text{\algebra}\{A\}](\text{\module}\{H\})$ : $\mathfrak{K}_{\mathcal{A}}(\mathcal{H})$  |
| <code>\opdomain</code>    | Domain of definition of an operator $\text{\opdomain}(A)$ : $\mathfrak{D}(A)$<br>Uses <code>hilbertfont</code> .   |
| <code>\spec</code>        | Spectrum of an operator $\text{\spec}(A)$ : $\text{spec}(A)$<br>Uses <code>operatorfont</code> .   |
| <code>\closure</code>     | Closure of an operator $\text{\closure}\{A\}$ : $\overline{A}$   |
| <code>\res</code>         | Resolvent set of an operator $\text{\res}(A)$ : $\text{res}(A)$  |

|                       |  |
|-----------------------|--|
|                       | Uses <code>operatorfont</code> .   |
| <code>\Res</code>     | Resolvent of an operator $\text{\Res}_z(A)$ : $\text{Res}_z(A)$                                  |
|                       | Uses <code>operatorfont</code> .   |
| <code>\specrad</code> | Spectral radius of an operator $\text{\specrad}(A)$ : $\varrho(A)$                               |
| <code>\slim</code>    | Strong limit $\text{\slim}_n \rightarrow \infty A_n$ : $\text{s-lim}_{n \rightarrow \infty} A_n$ |
| <code>\wlim</code>    | Weak limit $\text{\wlim}_n \rightarrow \infty A_n$ : $\text{w-lim}_{n \rightarrow \infty} A_n$   |

### 2.5.6 Dirac's Bra and Ket Notation

|                      |   |
|----------------------|---|
| <code>\bra</code>    | Dirac bra $\text{\bra}{\psi}$ : $\langle \psi  $                          |
| <code>\ket</code>    | Dirac ket $\text{\ket}{\phi}$ : $ \phi\rangle$                            |
| <code>\braket</code> | Dirac braket $\text{\braket}{\phi}{\psi}$ : $\langle \phi   \psi \rangle$ |
| <code>\ketbra</code> | Dirac ketbra $\text{\ketbra}{\phi}{\psi}$ : $ \phi\rangle\langle\psi $    |

### 2.5.7 Operator Algebras

|                    |   |
|--------------------|---|
| <code>\Spec</code> | Spectrum of an algebra $\text{\Spec}(\text{\algebra}{A})$ : $\text{Spec}(\mathcal{A})$    |
|                    | Uses <code>operatorfont</code> .  |
| <code>\Rad</code>  | Radical of an algebra $\text{\Rad}(\text{\algebra}{A})$ : $\text{Rad}(\mathcal{A})$       |
|                    | Uses <code>operatorfont</code> .  |
| <code>\ind</code>  | Fredholm index ( <code>\index</code> is already used!) $\text{\ind}(A)$ : $\text{ind}(A)$ |
|                    | Uses <code>operatorfont</code> .  |

### 2.5.8 Measure Theory and Integration

Here we need various function space of integrable functions (calligraphic ones) and the corresponding quotients by zero functions (roman ones):

|                          |   |
|--------------------------|---|
| <code>\Measurable</code> | Measurable functions $\text{\Measurable}(X)$ : $\mathcal{M}(X)$   |
|                          | Uses <code>operatorfont</code> .  |
| <code>\Meas</code>       | Complex measures $\text{\Meas}(X)$ : $\text{Meas}(X)$   |
|                          | Uses <code>operatorfont</code> .  |
| <code>\BoundMeas</code>  | Bounded measurable functions $\text{\BoundMeas}(X)$ : $\mathcal{BM}(X)$   |
|                          | Uses <code>spacefont</code> .   |
| <code>\Lp</code>         | Equivalence classes of $p$ -integrable functions ( $p$ is an optional argument) $\text{\Lp}(X)$ :<br>$L^p(X)$ and $\text{\Lp}[q](X)$ : $L^q(X)$   |
| <code>\Lone</code>       | Equivalence classes of integrable functions $\text{\Lone}(X)$ : $L^1(X)$  |
| <code>\Ltwo</code>       | Equivalence classes of square integrable functions $\text{\Ltwo}(X)$ : $L^2(X)$   |
| <code>\Linfty</code>     | Equivalence classes of essentially bounded functions $\text{\Linfty}(X)$ : $L^\infty(X)$  |
| <code>\Intp</code>       | Space of $p$ -integrable functions $\text{\Intp}(X)$ : $\mathcal{L}^p(X)$ and with optional argument<br>$\text{\Intp}[q](X)$ : $\mathcal{L}^q(X)$ |
| <code>\Intone</code>     | Space of integrable functions $\text{\Intone}(X)$ : $\mathcal{L}^1(X)$  |
| <code>\Inttwo</code>     | Space of square integrable functions $\text{\Inttwo}(X)$ : $\mathcal{L}^2(X)$   |
| <code>\Intinfy</code>    | Space of essentially bounded functions $\text{\Intinfy}(X)$ : $\mathcal{L}^\infty(X)$   |
| <code>\essrange</code>   | Essential range $\text{\essrange}(f)$ : $\text{ess range}(f)$   |
|                          | Uses <code>operatorfont</code> .  |
| <code>\esssup</code>     | Essential supremum $\text{\esssup}(f)$ : $\text{ess sup}(f)$  |

|             |  |
|-------------|--|
|             | Uses <code>operatorfont</code> .                                   |
| \esssupnorm | Essential supremum norm \esssupnorm{f}: $\ f\ _{\text{ess sup}}$   |
|             | Uses <code>operatorfont</code> .                                   |
| \ac         | Absolutely continuous part of a measure \mu_\ac: $\mu_{\text{ac}}$ |
|             | Uses <code>scriptfont</code> .                                     |
| \sing       | Singular part of a measure \mu_\sing: $\mu_{\text{sing}}$          |
|             | Uses <code>scriptfont</code> .                                     |

### 2.5.9 Limits

|          |   |
|----------|---|
| \indlim  | Inductive (or direct) limit \indlim_{i \in I} A_i: $\text{ind lim}_{i \in I} A_i$     |
|          | Uses <code>operatorfont</code> .  |
| \projlim | Projective (or inverse) limit \projlim_{i \in I} A_i: $\text{proj lim}_{i \in I} A_i$ |
|          | Uses <code>operatorfont</code> .  |

## 2.6 Category Theory

### 2.6.1 General Category Theory

|               |  |
|---------------|--|
| \category     | Font for generic categories \category{C}: $\mathcal{C}$                    |
|               | Uses <code>categoryfont</code> .   |
| \categoryname | Font for specific categories \categoryname{FinSet}: FinSet                 |
|               | Uses <code>categorynamefont</code> .                                       |
| \functor      | Font for functors \functor{F}: $F$   |
|               | Uses <code>functorfont</code> .  |
| \groupoid     | Font for groupoids \groupoid{G}: $\mathfrak{G}$                            |
|               | Uses <code>groupoidfont</code> .   |
| \source       | Source of arrow \source(f): $\text{source}(f)$                             |
|               | Uses <code>operatorfont</code> .   |
| \target       | Target of arrow \target(f): $\text{target}(f)$                             |
|               | Uses <code>operatorfont</code> .   |
| \unit         | Unit map in groupoids \unit\colon M \rightarrow G: unit: $M \rightarrow G$ |
|               | Uses <code>operatorfont</code> .   |
| \opp          | Opposite category etc. \category{C}^\opp: $\mathcal{C}^{\text{opp}}$       |
|               | Uses <code>scriptfont</code> .   |
| \asso         | Natural transformation of associativity \asso: asso                        |
|               | Uses <code>operatorfont</code> .   |
| \Hom          | Homomorphisms \Hom(A, B): $\text{Hom}(A, B)$                               |
|               | Uses <code>operatorfont</code> .   |
| \End          | Endomorphisms \End(E): $\text{End}(E)$                                     |
|               | Uses <code>operatorfont</code> .   |
| \Aut          | (*)-Automorphisms \Aut(A): $\text{Aut}(A)$                                 |
|               | \Aut^*(A): ${}^*-\text{Aut}(A)$  |
|               | Uses <code>operatorfont</code> .   |
| \Iso          | (*)-Isomorphisms \Iso(A, B): $\text{Iso}(A, B)$                            |

|                     |  |
|---------------------|--|
|                     | <code>\Iso*(A, B):</code> ${}^*\text{-}\text{Iso}(A, B)$                           |
|                     | Uses <code>operatorfont</code> .   |
| <code>\Obj</code>   | Objects of a category <code>\Obj(\category{C})</code> : $\text{Obj}(\mathfrak{C})$ |
|                     | Uses <code>operatorfont</code> .   |
| <code>\Morph</code> | Morphisms of a category <code>\Morph(a, b)</code> : $\text{Morph}(a, b)$           |
|                     | Uses <code>operatorfont</code> .   |

### 2.6.2 Colimits

|                     |   |
|---------------------|---|
| <code>\colim</code> | Colimits of diagrams or functors: <code>\colim \functor{F}</code> : $\text{colim } F$ |
|---------------------|---|

## 2.7 Differential Geometry

### 2.7.1 General Macros in Differential Geometry

|                         |   |
|-------------------------|---|
| <code>\Lie</code>       | Lie derivative <code>\Lie_X f</code> : $\mathcal{L}_X f$                              |
| <code>\Schouten</code>  | Schouten bracket <code>\Schouten{X, Y}</code> : $[X, Y]_s$ .                          |
| <code>\Forms</code>     | Differential forms <code>\Forms(M)</code> : $\Omega(M)$                               |
| <code>\ZdR</code>       | DeRham cocycles <code>\ZdR(M, \mathbb{C})</code> : $Z_{\text{dR}}(M, \mathbb{C})$     |
|                         | Uses <code>operatorfont</code> .  |
| <code>\BdR</code>       | DeRham coboundaries <code>\BdR(M, \mathbb{C})</code> : $B_{\text{dR}}(M, \mathbb{C})$ |
|                         | Uses <code>operatorfont</code> .  |
| <code>\HdR</code>       | DeRham cohomology <code>\HdR(M, \mathbb{C})</code> : $H_{\text{dR}}(M, \mathbb{C})$   |
|                         | Uses <code>operatorfont</code> .  |
| <code>\Diffeo</code>    | Diffeomorphism group <code>\Diffeo(M)</code> : $\text{Diffeo}(M)$                     |
|                         | Uses <code>operatorfont</code> .  |
| <code>\Diffop</code>    | Differential operators <code>\Diffop(M)</code> : $\text{DiffOp}(M)$                   |
|                         | Uses <code>operatorfont</code> .  |
| <code>\loc</code>       | To be used as an index <code>M_\loc</code> : $M_{\text{loc}}$                         |
|                         | Uses <code>scriptfont</code> .  |
| <code>\germ</code>      | Germs of functions <code>\germ_p(f)</code> : $\text{germ}_p(f)$                       |
|                         | Uses <code>operatorfont</code> .  |
| <code>\prol</code>      | Prolongation map <code>\prol(f)</code> : $\text{prol}(f)$                             |
|                         | Uses <code>operatorfont</code> .  |
| <code>\NRbracket</code> | Nijenhuis-Richardson bracket <code>\NRbracket{a, b}</code> : $[a, b]_{\text{NR}}$     |
|                         | Uses <code>scriptfont</code> .  |
| <code>\FNbracket</code> | Frölicher-Nijenhuis bracket <code>\FNbracket{a, b}</code> : $[a, b]_{\text{FN}}$      |
|                         | Uses <code>scriptfont</code> .  |
| <code>\Manifolds</code> | The category of manifolds <code>\Manifolds</code> : $\text{Manifold}$                 |
|                         | Uses <code>categorynamefont</code> .  |

### 2.7.2 Lie Groups and Principal Fiber Bundles

|                         |   |
|-------------------------|---|
| <code>\lefttriv</code>  | Left trivialization <code>\lefttriv</code> : $\text{left}$    |
|                         | Uses <code>operatorfont</code> .                              |
| <code>\righttriv</code> | Right trivialization <code>\righttriv</code> : $\text{right}$ |
|                         | Uses <code>operatorfont</code> .                              |

|                          |   |
|--------------------------|---|
| <code>\Gau</code>        | Gauge group $\text{\Gau}(P)$ : $\text{Gau}(P)$<br>Uses <code>operatorfont</code> .  |
| <code>\Conn</code>       | Connection one-forms $\text{\Conn}(P)$ : $\text{Conn}(P)$<br>Uses <code>operatorfont</code> .   |
| <code>\ratio</code>      | Ratio map of principal fiber bundle $\text{\ratio}(u, v)$ : $r(u, v)$<br>Uses <code>operatorfont</code> .   |
| <code>\Parallel</code>   | Parallel transport $\text{\Parallel}_0 \rightarrow 1, \gamma(v)$ : $P_{0 \rightarrow 1, \gamma}(v)$<br>Uses <code>operatorfont</code> .   |
| <code>\CE</code>         | Chevalley-Eilenberg as index $C_\bullet$ : $C_{\text{CE}}$<br>Uses <code>scriptfont</code> .  |
| <code>\HCE</code>        | Chevalley-Eilenberg cohomology $\text{\HCE}(\text{\liealg}\{g\})$ : $H_{\text{CE}}(\mathfrak{g})$<br>Uses <code>operatorfont</code> .   |
| <code>\fund</code>       | Trivialization by fundamental vector fields $\text{\fund}$ : $\text{fund}$<br>Uses <code>operatorfont</code> .  |
| <code>\Universal</code>  | Universal enveloping algebra $\text{\Universal}(\text{\liealg}\{g\})$ : $U(\mathfrak{g})$<br>Uses <code>operatorfont</code> .   |
| <code>\BCH</code>        | BCH as small index $\sigma_{\text{BCH}}$ : $\sigma_{\text{BCH}}$<br>Uses <code>scriptfont</code> .  |
| <code>\LieGroups</code>  | The category of Lie groups $\text{\LieGroups}$ : $\text{LieGroup}$<br>Uses <code>categorynamefont</code> .  |
| <code>\Principal</code>  | The category of principal bundles $\text{\Principal}$ : $\text{Principal}$<br>Uses <code>categorynamefont</code> .  |
| <code>\GPrincipal</code> | The category of $G$ -principal bundles $\text{\GPrincipal}$ : $G\text{-Principal}$<br>or with optional structure group $\text{\GPrincipal}[H]$ : $H\text{-Principal}$<br>Uses <code>categorynamefont</code> . |
| <code>\Fiber</code>      | The category of fiber bundles $\text{\Fiber}$ : $\text{Fiber}$ Uses <code>categorynamefont</code> .   |
| <code>\FFiber</code>     | The category of fiber bundles with typical fiber $\text{\FFiber}$ : $F\text{-Fiber}$<br>or with specified typical fiber $\text{\FFiber}[X]$ : $X\text{-Fiber}$<br>Uses <code>categorynamefont</code> .        |
| <code>\Pin</code>        | The pin group $\text{\Pin}(q, p)$ : $\text{Pin}(p, q)$<br>Uses <code>groupfont</code> .   |
| <code>\Spin</code>       | The spin group $\text{\Spin}(q, p)$ : $\text{Spin}(p, q)$<br>Uses <code>groupfont</code> .  |

### 2.7.3 (Pseudo-) Riemannian Geometry

|                         |   |
|-------------------------|---|
| <code>\nablaLC</code>   | Levi-Civita covariant derivative $\text{\nabla}_{\text{LC}}_X Y$ : $\nabla_X^{\text{LC}} Y$<br>Uses <code>scriptfont</code> .                                   |
| <code>\Laplace</code>   | Laplace operator $\text{\Laplace} f$ : $\Delta f$   |
| <code>\dAlembert</code> | D'Alembert operator $\text{\dAlembert} u$ : $\square u$   |
| <code>\feynman</code>   | Feynman slash notation $\text{\feynman}\{D\} = \text{\feynman}\{A\} + \text{\feynman}\{\partial\}$ :<br>$\not{D} = \not{A} + \not{\partial}$                    |
| <code>\Dirac</code>     | Dirac operator $\text{\Dirac} u$ : $\not{D} u$  |
| <code>\rotation</code>  | Rotation (i.e. curl) of a vector field $\text{\rotation}(X)$ : $\text{rot}(X)$ . Not to be confused with $\text{grün}(X)$ .<br>Uses <code>operatorfont</code> . |

|                          |  |
|--------------------------|--|
| <code>\curl</code>       | Curl of a vector field $\curl \vec{X}$ : $\operatorname{curl} \vec{X}$<br>Uses <code>operatorfont</code> .   |
| <code>\divergence</code> | Divergence of a vector field $\operatorname{div}(X)$ : $\operatorname{div}(X)$<br>Uses <code>operatorfont</code> .   |
| <code>\gradient</code>   | Gradient of a function $\operatorname{grad} f$ : $\operatorname{grad} f$<br>Uses <code>operatorfont</code> .   |
| <code>\Tor</code>        | Torsion of a covariant derivative $\operatorname{Tor}(X, Y)$ : $\operatorname{Tor}(X, Y)$<br>Uses <code>operatorfont</code> .  |
| <code>\Ric</code>        | Ricci curvature $\operatorname{Ric}(X, Y)$ : $\operatorname{Ric}(X, Y)$<br>Uses <code>operatorfont</code> .  |
| <code>\scal</code>       | Scalar curvature $\operatorname{scal}$ : $\operatorname{scal}$<br>Uses <code>operatorfont</code> .   |
| <code>\Riem</code>       | The set of Riemannian metrics (linear and on manifolds) $\operatorname{Riem}(M)$ : $\operatorname{Riem}(M)$<br>Uses <code>operatorfont</code> .  |
| <code>\Hessian</code>    | Hessian of a function $\operatorname{Hessian}(f)$ $\in \operatorname{Sec}^{\infty}(\operatorname{Sym}^2 T^* M)$ : $\operatorname{Hessian}(f) \in \Gamma^\infty(S^2 T^* M)$<br>Uses <code>operatorfont</code> . |
| <code>\hodge</code>      | Hodge star operator $\alpha \mapsto \operatorname{hodge}\alpha$ : $\alpha \mapsto \star \alpha$  |

#### 2.7.4 Complex Geometry

|                         |  |
|-------------------------|--|
| <code>\Nijenhuis</code> | Nijenhuis operator $\operatorname{Nijenhuis}(X, Y)$ : $\operatorname{Nij}(X, Y)$<br>Uses <code>operatorfont</code> . |
| <code>\del</code>       | Dolbeault operator $\partial\bar{\omega}$ : $\partial\bar{\omega}$   |
| <code>\delbar</code>    | CC of Dolbeault operator $\operatorname{delbar}\alpha$ : $\bar{\partial}\alpha$                                      |
| <code>\FS</code>        | Fubini Study as very small index $\omega_{\text{FS}}$ : $\omega_{\text{FS}}$<br>Uses <code>scriptfont</code> .       |

#### 2.7.5 Vector Bundles

|                        |   |
|------------------------|---|
| <code>\Lift</code>     | Generic lift of something $\nabla^{\operatorname{Lift}}$ : $\nabla^{\operatorname{Lift}}$<br>Uses <code>scriptfont</code> . |
| <code>\ver</code>      | Vertical lift $X^{\operatorname{ver}}$ : $X^{\operatorname{ver}}$<br>Uses <code>scriptfont</code> .                         |
| <code>\hor</code>      | Horizontal lift $X^{\operatorname{hor}}$ : $X^{\operatorname{hor}}$<br>Uses <code>scriptfont</code> .                       |
| <code>\Ver</code>      | Vertical subbundle $\operatorname{Ver}(E)$ : $\operatorname{Ver}(E)$<br>Uses <code>operatorfont</code> .                    |
| <code>\Hor</code>      | Horizontal subbundle $\operatorname{Hor}(E)$ : $\operatorname{Hor}(E)$<br>Uses <code>operatorfont</code> .                  |
| <code>\Sec</code>      | $C^k$ -sections $\operatorname{Sec}(E)$ : $\Gamma^k(E)$ and $\operatorname{Sec}[2](E)$ : $\Gamma^2(E)$                      |
| <code>\Secinfty</code> | Smooth sections $\operatorname{Sec}^{\infty}(E)$ : $\Gamma^\infty(E)$   |
| <code>\HolSec</code>   | Holomorphic sections $\operatorname{HolSec}(U, E)$ : $\Gamma_{\text{hol}}(U, E)$<br>Uses <code>scriptfont</code> .          |
| <code>\SymD</code>     | Symmetrized covariant derivative $\operatorname{SymD}^n f$ : $D^n f$<br>Uses <code>operatorfont</code> .                    |

|                                  |   |
|----------------------------------|---|
| <code>\Densities</code>          | Densities of a vector bundle of rank $n$ or specific rank $\text{\Densities } TM:  \Lambda^n TM$ and $\text{\Densities}[k]^{\alpha} E:  \Lambda^k ^{\alpha} E$ .  |
| <code>\MeasurableSections</code> | Measurable sections $\text{\MeasurableSections}(E): \mathcal{M}\Gamma(E)$<br>Uses <code>spacefont</code> .  |
| <code>\IntpSections</code>       | $p$ -Integrable Sections $\text{\IntpSections}(\text{\Densities } T^*M): \mathcal{L}^p\Gamma( \Lambda^n T^*M)$ or with optional argument $\text{\IntpSections}[q](\text{\Densities } T^*M): \mathcal{L}^q\Gamma( \Lambda^n T^*M)$ . |
| <code>\IntegrableSections</code> | Integrable sections $\text{\IntegrableSections}(\text{\Densities } T^*M): \mathcal{L}^1\Gamma( \Lambda^n T^*M)$   |
| <code>\Translation</code>        | Fiber translations $\text{\Translation}_A: T_A$<br>Uses <code>operatorfont</code> .   |
| <code>\frames</code>             | Font for local frames $\text{\frames}\{e\}_1, \dots, \text{\frames}\{e\}_k: e_1, \dots, e_k$<br>Uses <code>operatorfont</code> .  |
| <code>\Frames</code>             | Frame bundle of a vector bundle $\text{\Frames}(E) \rightarrow M$ :<br>$\text{\Frames}(E) \longrightarrow M$<br>Uses <code>operatorfont</code> .  |
| <code>\FDiff</code>              | Fiber derivative $\text{\FDiff } L: FL$<br>Uses <code>operatorfont</code> .   |

### 2.7.6 Symplectic and Poisson Geometry

|                           |   |
|---------------------------|---|
| <code>\Symp</code>        | Symplectomorphism group $\text{\Symp}(M, \omega): \text{Symp}(M, \omega)$<br>Uses <code>groupfont</code> .                            |
| <code>\Jacobiator</code>  | Jacobiator $\text{\Jacobiator}: \text{Jac}_{\pi}$ and $\text{\Jacobiator}[\nu]: \text{Jac}_{\nu}$<br>Uses <code>operatorfont</code> . |
| <code>\red</code>         | Reduced as an index $M_{\red}: M_{\text{red}}$<br>Uses <code>scriptfont</code> .  |
| <code>\Hess</code>        | Hess map $\text{\Hess}: \text{Hess}(\nabla)$<br>Uses <code>operatorfont</code> .  |
| <code>\KKS</code>         | KKS as tiny index $\{f, g\}_{\KKS}: \{f, g\}_{\text{KKS}}$<br>Uses <code>scriptfont</code> .  |
| <code>\Courant</code>     | Courant bracket $\text{\Courant}\{a, b\}: [a, b]_C$<br>Uses <code>scriptfont</code> .   |
| <code>\Dorfman</code>     | Dorfman bracket $\text{\Dorfman}\{(x, \xi), (y, \eta)\}: [(x, \xi), (y, \eta)]_D$<br>Uses <code>scriptfont</code> .                   |
| <code>\Dir</code>         | (Linear) Dirac structures $\text{\Dir}(V): \text{Dir}(V)$<br>Uses <code>operatorfont</code> .   |
| <code>\Forward</code>     | Forward map $\text{\Forward}(\phi): \mathcal{F}(\phi)$  |
| <code>\Backward</code>    | Backward map $\text{\Backward}(\phi): \mathcal{B}(\phi)$  |
| <code>\Tangent</code>     | Generalized tangent bundle/map $\text{\Tangent } M: \mathbb{T}M$  |
| <code>\MWreduction</code> | Marsden-Weinstein reduction $M \text{\MWreduction } G: M//G$  |
| <code>\Mon</code>         | Monodromy groupoid $\text{\Mon}(M): \text{Mon}(M)$<br>Uses <code>operatorfont</code> .  |
| <code>\Hol</code>         | Holonomy groupoid $\text{\Hol}(M): \text{Hol}(M)$<br>Uses <code>operatorfont</code> .   |

## 2.8 Linear Algebra

### 2.8.1 General Linear Algebra

|         |  |
|---------|--|
| \tr     | Trace of a linear map \tr(A): $\text{tr}(A)$<br>Uses <code>operatorfont</code> .   |
| \rank   | Rank of a linear map \rank(A): $\text{rank}(A)$<br>Uses <code>operatorfont</code> .  |
| \codim  | Codimension \codim U: $\text{codim } U$<br>Uses <code>operatorfont</code> .  |
| \diag   | Diagonal (for filling matrices etc.) \diag(1,-1, -1): $\text{diag}(1, -1, -1)$<br>Uses <code>operatorfont</code> .   |
| \Trans  | Transposition of matrices A^\Trans: $A^T$<br>Uses <code>scriptfont</code> .  |
| \Mat    | Matrices \Mat_n(\mathbb{R}): $M_n(\mathbb{R})$<br>Uses <code>operatorfont</code> .   |
| \SymMat | Symmetric matrices \SymMat_n(\mathbb{R}): $\text{SymMat}_n(\mathbb{R})$<br>Uses <code>operatorfont</code> .  |
| \ann    | Annihilator of a subspace U^\ann: $U^{\text{ann}}$<br>Uses <code>scriptfont</code> .   |
| \Span   | Span of something \Span\{v, u\}: $\text{span}\{v, u\}$ and with optional argument<br>\Span[\mathbb{C}]\{v, u\}: $\text{span}_{\mathbb{C}}\{v, u\}$<br>Uses <code>operatorfont</code> . |
| \basis  | Font for basis vectors \basis{e}_i: $e_i$<br>Uses <code>basisfont</code> .   |

### 2.8.2 Tensors

|                  |   |
|------------------|---|
| \tensor          | Generic tensor product over some ring a \tensor b: $a \otimes b$ .<br>With optional subscript V \tensor[\algebra{A}]: $V \otimes_{\mathcal{A}} U$ |
| \Tensor          | Tensor powers, tensor algebra \Tensor^\bullet(V): $T^\bullet(V)$<br>Uses <code>operatorfont</code> .  |
| \Anti            | Antisymmetric tensor powers, Grassmann algebra \Anti(V): $\Lambda(V)$   |
| \Sym             | Symmetric tensor powers, symmetric algebra \Sym^\bullet(V): $S^\bullet(V)$<br>Uses <code>operatorfont</code> .                                    |
| \Symmetrizer     | Symmetrizer \Symmetrizer_n: $\text{Sym}_n$  |
| \AntiSymmetrizer | Anti-symmetrizer \AntiSymmetrizer: Alt  |
| \ins             | Generic insertion map \ins_X: $i_X$<br>Uses <code>operatorfont</code> .   |
| \jns             | Generic right insertion map \jns_X: $j_X$<br>Uses <code>operatorfont</code> .   |
| \insa            | Antisymmetric insertion map \insa(X): $i_a(X)$<br>Uses <code>operatorfont, scriptfont</code> .  |
| \inss            | Symmetric insertion map \inss(v): $i_s(v)$<br>Uses <code>operatorfont, scriptfont</code> .  |
| \dega            | Antisymmetric degree \dega(a) = ka: $\deg_a(a) = ka$<br>Uses <code>operatorfont, scriptfont</code> .  |

`\degs` Symmetric degree  $\text{\degs}(X) = \text{\ell}_\text{ell} X$ :  $\deg_s(X) = \ell X$   
 Uses `operatorfont`, `scriptfont`.

### 2.8.3 Inner Products

`\SP` Simple scalar product  $\text{\SP}\{x, y\}: \langle x, y \rangle$ .  
`\littlepara` Small parallel to be used as a subscript  $v_{\text{\littlepara}}$ :  $v_{\parallel}$   
`\IP` Generic inner product with five arguments to decorate it  $\text{\IP}[\cdot]\{\cdot\}\{\cdot\}\{\cdot\}$  and  
 an optional argument to adjust the size:

$${}_B\langle z, w \rangle_R^\perp \quad \text{and} \quad {}_{\mathcal{B}}^{\perp} \left\langle \prod x_i, y \right\rangle_{\mathcal{A}}'$$

## 2.9 Statistics

### 2.9.1 Macros for General Statistics

`\EX` Expectation value  $\text{\EX}_{\omega}(A)$ :  $E_\omega(A)$   
 Uses `operatorfont`.  
`\Var` Variance  $\text{\Var}(a)$ :  $\text{Var}(a)$   
 Uses `operatorfont`.  
`\Cov` Covariance  $\text{\Cov}_{\omega}(a, b)$ :  $\text{Cov}_\omega(a, b)$   
 Uses `operatorfont`.  
`\Cor` Correlation  $\text{\Cor}(a, b)$ :  $\text{Cor}(a, b)$   
 Uses `operatorfont`.

## 2.10 Topology

### 2.10.1 Macros for Topology

`\cl` Topological closure  $X^{\text{\cl}}$ :  $X^{\text{cl}}$   
 Uses `scriptfont`.  
`\scl` Sequential closure  $A^{\text{\scl}}$ :  $A^{\text{scl}}$   
 Uses `scriptfont`.  
`\interior` Open interior  $A^{\text{\interior}}$ :  $A^\circ$   
`\boundary` Boundary of a subset  $\text{\boundary}_A$ :  $\partial A$   
`\supp` Support of a function  $\text{\supp}_f$ :  $\text{supp } f$   
 Uses `operatorfont`.  
`\dist` Distance  $\text{\dist}(p, A)$ :  $\text{dist}(p, A)$   
 Uses `operatorfont`.  
`\topology` Font for topology  $\text{\topology}\{M\}$ :  $\mathcal{M}$   
 Uses `topologyfont`.  
`\filter` Font for filter  $\text{\filter}\{F\}$ :  $\mathfrak{F}$   
 Uses `filterfont`.  
`\sheaf` Font for sheaves  $\text{\sheaf}\{F\}$ :  $\mathcal{F}$   
 Uses `sheaffont`.

|                        |   |
|------------------------|---|
| <code>\Sections</code> | Discontinuous sections of a presheaf <code>\Sections(\sheaf{F})</code> : $\text{Sections}(\mathcal{F})$<br>Uses <code>operatorfont</code> .   |
| <code>\HOM</code>      | Sheaf of morphisms between sheaves <code>\HOM(\sheaf{F}, \sheaf{G})</code> : $\mathcal{H}\text{om}(\mathcal{F}, \mathcal{G})$<br>Uses <code>sheaffont</code> and <code>\mathit</code> . |
| <code>\etale</code>    | Étalé space of presheaf <code>\etale{\sheaf{F}}</code> : $ \mathcal{F} $ .  |

### 2.10.2 Categories from Topology

|                           |  |
|---------------------------|--|
| <code>\topological</code> | Category of topological spaces <code>\topological</code> : $\text{top}$<br>Uses <code>categoryname</code> .                  |
| <code>\Topological</code> | Category of Hausdorff topological spaces <code>\Topological</code> : $\text{Top}$<br>Uses <code>categoryname</code> .        |
| <code>\Sheaves</code>     | Category of sheaves over a space <code>\Sheaves(M)</code> : $\text{Sheaves}(M)$<br>Uses <code>categoryname</code> .          |
| <code>\PreSheaves</code>  | Category of presheaves over a space <code>\PreSheaves(M)</code> : $\text{PreSheaves}(M)$<br>Uses <code>categoryname</code> . |
| <code>\Etale</code>       | Category of étalé spaces over a space <code>\Etale(M)</code> : $\text{Etale}(M)$<br>Uses <code>categoryname</code> .         |

## 3 Implementation

The following packages are required:

```

1 \RequirePackage{amsmath}
2 \RequirePackage{amsymb}
3 \RequirePackage{mathtools}
```

Grab only those fonts from `stmry` which we actually need

```

4 \DeclareSymbolFont{stmry}{U}{stmry}{m}{n}
5 \SetSymbolFont{stmry}{bold}{U}{stmry}{b}{n}
6 \RequirePackage{xkeyval}
```

Used for allowing key-value pairs as options.

```
7 \RequirePackage{tensor}
```

The `suffix` package allows to define `*`-versions of macros.

```
8 \RequirePackage{suffix}
```

In order to get the package options for `nchairx` working, the following needs to be defined.

```
9 \newif\if@loadmath \if@loadmathtrue
```

### 3.1 Fonts

First we check of macros should be included:

```
10 \if@loadmath
```

We provide several font names for easier usage and customization. The fonts are used in our macro definitions and can be changed by according to the individual needs.

### 3.1.1 Default Values for some Math Fonts

|          |   |
|----------|---|
| \mathbb  | Redefine \mathbb to use the nicer \mathbbm.               |
|          | 11 \DeclareMathAlphabet{\ch@airxmathbbm}{U}{bbm}{m}{n}    |
|          | 12 \SetMathAlphabet{\ch@airxmathbbm}{bold}{U}{bbm}{bx}{n} |
|          | 13 \renewcommand{\mathbbb}[1]{\ch@airxmathbbm{#1}}        |
| \mathscr | We load a script font and provide the command \mathscr    |
|          | 14 \DeclareMathAlphabet{\mathscr}{U}{rsfso}{m}{n}         |
| \mathcal | We redefine the \mathcal command using the Euler font.    |
|          | 15 \DeclareSymbolFont{EulerScript}{U}{eus}{m}{n}          |
|          | 16 \SetSymbolFont{EulerScript}{bold}{U}{eus}{b}{n}        |
|          | 17 \DeclareSymbolFontAlphabet{\mathcal}{EulerScript}      |

### 3.1.2 Setting Fonts for Various Math Groups

Definitions of fonts for the different groups.

|                         |   |
|-------------------------|---|
| \ch@irxalgebrafont      |   |
| \ch@irxbasisfont        |   |
| \ch@irxcategoryfont     |   |
| \ch@irxcategorynamefont | 18 \define@key[chairx]{fonts}{algebrafont}{       |
| \ch@irxfieldfont        | 19 \providecommand{\ch@irxalgebrafont}[1]{ }      |
| \ch@irxfILTERfont       | 20 \renewcommand{\ch@irxalgebrafont}{#1}          |
| \ch@irxfunctorfont      | 21 }  |
| \ch@irxgerstenhaberfont | 22 \define@key[chairx]{fonts}{basisfont}{         |
| \ch@irxgroupfont        | 23 \providecommand{\ch@irxbasisfont}[1]{ }        |
| \ch@irxgroupoidfont     | 24 \renewcommand{\ch@irxbasisfont}{#1}            |
| \ch@irxhilbertfont      | 25 }  |
| \ch@irxliealgonft       | 26 \define@key[chairx]{fonts}{categoryfont}{      |
| \ch@irxmodulefont       | 27 \providecommand{\ch@irxcategoryfont}[1]{ }     |
| \ch@irxprehilbfont      | 28 \renewcommand{\ch@irxcategoryfont}{#1}         |
| \ch@irxoperatorfont     | 29 }  |
| \ch@irxringfont         | 30 \define@key[chairx]{fonts}{categorynamefont}{  |
| \ch@irxscriptfont       | 31 \providecommand{\ch@irxcategorynamefont}[1]{ } |
| \ch@irxsheaffont        | 32 \renewcommand{\ch@irxcategorynamefont}{#1}     |
| \ch@irxspacesfont       | 33 }  |
| \ch@irxtopologyfont     | 34 \define@key[chairx]{fonts}{fieldfont}{         |
|                         | 35 \providecommand{\ch@irxfieldfont}[1]{ }        |
|                         | 36 \renewcommand{\ch@irxfieldfont}{#1}            |
|                         | 37 }  |
|                         | 38 \define@key[chairx]{fonts}{filterfont}{        |
|                         | 39 \providecommand{\ch@irxfILTERfont}[1]{ }       |
|                         | 40 \renewcommand{\ch@irxfILTERfont}{#1}           |
|                         | 41 }  |
|                         | 42 \define@key[chairx]{fonts}{functorfont}{       |
|                         | 43 \providecommand{\ch@irxfunctorfont}[1]{ }      |
|                         | 44 \renewcommand{\ch@irxfunctorfont}{#1}          |

```

45 }
46 \define@key[chairx]{fonts}{gerstenhaberfont}{
47 \providecommand{\ch@irxgerstenhaberfont}[1]{ }
48 \renewcommand{\ch@irxgerstenhaberfont}{#1}
49 }
50 \define@key[chairx]{fonts}{groupfont} {
51 \providecommand{\ch@irxgroupfont}[1]{ }
52 \renewcommand{\ch@irxgroupfont}{#1}
53 }
54 \define@key[chairx]{fonts}{groupoidfont} {
55 \providecommand{\ch@irxgroupoidfont}[1]{ }
56 \renewcommand{\ch@irxgroupoidfont}{#1}
57 }
58 \define@key[chairx]{fonts}{hilbertfont} {
59 \providecommand{\ch@irxhilbertfont}[1]{ }
60 \renewcommand{\ch@irxhilbertfont}{#1}
61 }
62 \define@key[chairx]{fonts}{liealgonfont} {
63 \providecommand{\ch@irxliealgonfont}[1]{ }
64 \renewcommand{\ch@irxliealgonfont}{#1}
65 }
66 \define@key[chairx]{fonts}{modulefont} {
67 \providecommand{\ch@irxmodulefont}[1]{ }
68 \renewcommand{\ch@irxmodulefont}{#1}
69 }
70 \define@key[chairx]{fonts}{prehilbfont} {
71 \providecommand{\ch@irxprehilbfont}[1]{ }
72 \renewcommand{\ch@irxprehilbfont}{#1}
73 }

```

Here we need to change the default operatorfont in order to get the chairxoperatorfont also for `\operatorname` and `\DeclareMathOperator`. Note that redefining `\operatorname@font` with a symbol alphabet and not a symbol font forces us to use an additional bracket in all definitions using `\operatorname` and `\DeclareMathOperator`.

```

74 \define@key[chairx]{fonts}{operatorfont} {
75     \providecommand{\ch@irxoperatorfont}[1]{ }
76     \renewcommand{\ch@irxoperatorfont}{#1}
77 }
78 \define@key[chairx]{fonts}{ringfont} {
79 \providecommand{\ch@irxringfont}[1]{ }
80 \renewcommand{\ch@irxringfont}{#1}
81 }
82 \define@key[chairx]{fonts}{scriptfont} {
83     \providecommand{\ch@irxscriptfont}[1]{ }
84     \renewcommand{\ch@irxscriptfont}{#1}
85 }
86 \define@key[chairx]{fonts}{sheaffont} {
87 \providecommand{\ch@irxsheaffont}[1]{ }
88 \renewcommand{\ch@irxsheaffont}{#1}

```

```

89 }
90 \define@key[chairx]{fonts}{spacefont}{
91     \providecommand{\ch@irxspacefont}[1]{ }
92     \renewcommand{\ch@irxspacefont}{#1}
93 }
94 \define@key[chairx]{fonts}{topologyfont}{
95 \providecommand{\ch@irxtopologyfont}[1]{ }
96 \renewcommand{\ch@irxtopologyfont}{#1}
97 }

\chairxfonts Command for setting the fonts.
98 \newcommand{\chairxfonts}[1]{
99   \setkeys[chairx]{fonts}{#1}
100 }
```

We use the following default settings for fonts.

```

101 \chairxfonts{
102   algebrafont = \mathscr,
103   basisfont = \mathit,
104   categoryfont = \mathfrak,
105   categorynamefont = \mathsf,
106   fieldfont = \mathbb,
107   filterfont = \mathfrak,
108   functorfont = \mathsf,
109   groupfont = \mathrm,
110   groupoidfont = \mathfrak,
111   gerstenhaberfont = \mathfrak,
112   hilbertfont = \mathfrak,
113   liealgefont = \mathfrak,
114   modulefont = \mathscr,
115   prehilbfont = \mathcal,
116   operatorfont = \mathrm,
117   ringfont = \mathsf,
118   scriptfont = \mathrm,
119   sheaffont = \mathscr,
120   spacefont = \mathscr,
121   topologyfont = \mathscr
122 }
```

code for grabbing a single glyph from some random font without investing a new math alphabet: use only the wrapper macro as `\ch@irxmathsymbol[mathtype]{fontname}{glyph}` with `mathtype` being the optional type of the symbol with default being `\mathord`, `fontname` the name of the font where the symbol is to be found and `glyph` the number of the symbol inside the specified font.

```

123 \newcommand{\ch@irxfont}[1]{\fontfamily{#1}\fontencoding{U}\fontseries{m}\fontshape{n}\selectfont}
124 \newcommand{\ch@irxsymbol}[2]{\{\ch@irxfont{#1}\char#2\}}
125 \newcommand{\ch@irxmathsymbol}[3]{[\mathord]{%
126   #1{\ch@irxm@thsymbol{#2}{#3}}}}
127 \def\ch@irxm@thsymbol#1#2{\mathchoice
```

```

128  {\@ch@irxm@thsymbol{#1}{#2}\tf@size}
129  {\@ch@irxm@thsymbol{#1}{#2}\tf@size}
130  {\@ch@irxm@thsymbol{#1}{#2}\sf@size}
131  {\@ch@irxm@thsymbol{#1}{#2}\ssf@size}}
132 \def\@ch@irxm@thsymbol#1#2#3{\mbox{\fontsize{#3}{#3}\ch@irxsymbol{#1}{#2}}}
133 %
134 \fi

```

## 3.2 New Delimiters

First we check of macros should be included:

```
135 \if@loadmath
```

### 3.2.1 The New Delimiters

```

\vast Bigger than \Bigg commands for explicit re-sizing brackets and things needs
\Vast left/right version to work with \DeclarePairedDelimiters. Hack from http://tex.stackexchange.com/que
\vastl 136 \newcommand{\vast}{\bBigg@{4}}
\vastm 137 \newcommand{\Vast}{\bBigg@{5}}
\vastr 138 \newcommand{\vastl}{\mathopen\vast}
\Vastl 139 \newcommand{\vastm}{\mathrel\vast}
\Vastm 140 \newcommand{\vastr}{\mathclose\vast}
\Vastr 141 \newcommand{\Vastl}{\mathopen\Vast}
142 \newcommand{\Vastm}{\mathrel\Vast}
143 \newcommand{\Vastr}{\mathclose\Vast}

144 \fi

```

## 3.3 General Mathematics Macros

First we check of macros should be included:

```
145 \if@loadmath
```

### 3.3.1 General Math Commands

```

\I
146 \newcommand{\I}{\mathrm{i}}
\E
147 \newcommand{\E}{\mathrm{e}}
\mathop{!}
148 \newcommand{\D}{\mathop{!}\mathrm{d}}
\overline{ }
149 \newcommand{\cc}[1]{\overline{#1}}

```



```

\inv
165 \newcommand{\inv}{\operatorname{\ch@irxoperatorfont{inv}}}

\ev
166 \newcommand{\ev}{\operatorname{\ch@irxoperatorfont{ev}}}

\image
167 \newcommand{\image}{\operatorname{\ch@irxoperatorfont{im}}}

\graph
168 \newcommand{\graph}{\operatorname{\ch@irxoperatorfont{graph}}}

\coimage
169 \newcommand{\coimage}{\operatorname{\ch@irxoperatorfont{coim}}}

\coker
170 \newcommand{\coker}{\operatorname{\ch@irxoperatorfont{coker}}}

\operator
171 \newcommand{\operator}[1]{\operatorname{\ch@irxoperatorfont{#1}}}

```

### 3.3.4 Relations

```

\later
172 \newcommand{\later}{\mathrel{\succcurlyeq} }

\earlier
173 \newcommand{\earlier}{\mathrel{\preccurlyeq} }

```

### 3.3.5 Sums and Products

- \bigop** To define sum-like operators that are scaled up in displaystyle we define the following command taken from [tex.stackexchange.com/questions/23432/how-to-create-my-own-math-operator-with-limits](https://tex.stackexchange.com/questions/23432/how-to-create-my-own-math-operator-with-limits)
- ```

174 \DeclareRobustCommand{\bigop}[2][1]{%
175 \mathop{\vphantom{\sum}\mathpalette\bigop@{{#1}{#2}}}\limits@%
176 }%
177 \newcommand{\bigop@}[2]{\bigop@@#1#2}%
178 \newcommand{\bigop@@}[3]{%
179 \vcenter{%
180 \sbox{z@\$#1\sum\$}%
181 \hbox{\resizebox{\ifx#1\displaystyle#2\fi\dimexpr\ht{z@}+\dp{z@}\fi\!}{\$m@th#3\$}}%
182 }%
183 }

```
- \bigplus** The command `\DOTSB` is used for correct behaviour of `\dots` before or after the command.
- ```

184 \newcommand{\bigplus}{\DOTSB\bigop{+}}

```

```

\bigtimes
185 \newcommand{\bigtimes}{\DOTSB\big@p{\times}}
\biprod
186 \newcommand{\biprod}{\DOTSB\big@p{\mathrel{\prod\hspace{-0.4cm}\coprod}}}

```

### 3.3.6 Labels

Smiley from `wasy`

```

\smiley
187 \newcommand{\smiley}{\ch@irxmathsymbol[\mathord]{wasy}{44}}

```

Frownie from `wasy`

```

\frownie
188 \newcommand{\frownie}{\ch@irxmathsymbol[\mathord]{wasy}{47}}
\heart
189 \newcommand{\heart}{\heartsuit}
190 \fi

```

## 3.4 Algebra

First we check of macros should be included:

```
191 \if@loadmath
```

### 3.4.1 Fonts for Rings and Things

```

\field
192 \newcommand{\field}[1]{\ch@irxfieldfont{#1}}
\ring
193 \newcommand{\ring}[1]{\ch@irxringfont{#1}}
\group
194 \newcommand{\group}[1]{\ch@irxgroupfont{#1}}
\algebra
195 \newcommand{\algebra}[1]{\ch@irxalgebrafont{#1}}
\module
196 \newcommand{\module}[1]{\ch@irxmodulefont{#1}}
\liealg
197 \newcommand{\liealg}[1]{\ch@irxliealgonft{#1}}

```

```

\MC
198 \newcommand{\MC}{\scriptscriptstyle\ch@irxscriptfont{MC}{}}

\gerstenhaber
199 \newcommand{\gerstenhaber}[1] {\ch@irxgerstenhaberfont{#1}{}}

3.4.2 Some Symbols needed in Algebra

\Pol
200 \newcommand{\Pol}{\ch@irxoperatorfont{Pol}{}}

\lmult
201 \newcommand{\lmult}{\operatorname{\ch@irxoperatorfont{\ell}}{}}

\rmult
202 \newcommand{\rmult}{\operatorname{\ch@irxoperatorfont{r}}{}}

\Lmult
203 \newcommand{\Lmult}{\operatorname{\ch@irxoperatorfont{L}}{}}

\Rmult
204 \newcommand{\Rmult}{\operatorname{\ch@irxoperatorfont{R}}{}}

\Center Needs mathrsfs package.
205 \newcommand{\Center}{\mathscr{Z}{}}

\ad
206 \newcommand{\ad}{\operatorname{\ch@irxoperatorfont{ad}}{}}

\Ad
207 \newcommand{\Ad}{\operatorname{\ch@irxoperatorfont{Ad}}{}}

\Conj
208 \newcommand{\Conj}{\operatorname{\ch@irxoperatorfont{Conj}}{}}

\acts
209 \newcommand{\acts}{\mathbin{\triangleright}{}}

\racts
210 \newcommand{\racts}{\mathbin{\triangleleft}{}}

\Char
211 \newcommand{\Char}{\ch@irxoperatorfont{char}{}}

\modulo
212 \newcommand{\modulo}{\operatorname{\ch@irxoperatorfont{mod}}{}}

```

```

\Clifford
213 \newcommand{\Clifford}{\operatorname{\ch@irxoperatorfont{Cl}}}

\cClifford
214 \newcommand{\cClifford}{\operatorname{\mathbb{C}\ch@irxoperatorfont{l}}}

\Der
215 \newcommand{\Der}{\operatorname{\ch@irxoperatorfont{Der}}}
216 \WithSuffix\newcommand\Der*{\decoration{^*}{\text{--}}\Der{}}

\InnDer
217 \newcommand{\InnDer}{\operatorname{\ch@irxoperatorfont{InnDer}}}
218 \WithSuffix\newcommand\InnDer*{\decoration{^*}{\text{--}}\InnDer{}}

\OutDer
219 \newcommand{\OutDer}{\operatorname{\ch@irxoperatorfont{OutDer}}}
220 \WithSuffix\newcommand\OutDer*{\decoration{^*}{\text{--}}\OutDer{}}

\InnAut
221 \newcommand{\InnAut}{\operatorname{\ch@irxoperatorfont{InnAut}}}
222 \WithSuffix\newcommand\InnAut*{\decoration{^*}{\text{--}}\InnAut{}}

\OutAut
223 \newcommand{\OutAut}{\operatorname{\ch@irxoperatorfont{OutAut}}}
224 \WithSuffix\newcommand\OutAut*{\decoration{^*}{\text{--}}\OutAut{}}

\formal
225 \newcommand{\formal}[1]{\ch@irxllbracket #1\ch@irxrbracket}

\laurent
226 \newcommand{\laurent}[1]{(\!\!(#1)\!\!)}

\sweedler
227 \newcommand{\sweedler}[1]{\scriptscriptstyle(#1)}

```

### 3.4.3 Categories from Algebra

```

\algebras
228 \newcommand{\algebras}{\categoryname{alg}}
229 \WithSuffix\newcommand\algebras*{\decoration{^*}{\text{--}}\algebras{}}

\Algebras
230 \newcommand{\Algebras}{\categoryname{Alg}}
231 \WithSuffix\newcommand\Algebras*{\decoration{^*}{\text{--}}\Algebras{}}

\reps
232 \newcommand{\reps}{\categoryname{rep}}
233 \WithSuffix\newcommand\reps*{\decoration{^*}{\text{--}}\reps{}}

```

```

\RReps
234 \newcommand{\RReps}{\categoryname{Rep}}
235 \WithSuffix\newcommand\RReps*{\decoration{^*}{\textrm{-}}\RReps{}}

\PoissonAlg
236 \newcommand{\PoissonAlg}{\categoryname{PoissonAlg}}
237 \WithSuffix\newcommand\PoissonAlg*{\decoration{^*}{\textrm{-}}\PoissonAlg{}}

\modules
238 \newcommand{\modules}{\categoryname{mod}}
239 \WithSuffix\newcommand\modules*{\decoration{^*}{\textrm{-}}\modules{}}

\Leftmodules
240 \newcommand{\Leftmodules}[1]{\textsf{-}\categoryname{mod}{}}

\Rightmodules
241 \newcommand{\Rightmodules}[2]{\categoryname{mod}_{}\#1\textsf{-}\#2\categoryname{mod}{}}

\Modules
242 \newcommand{\Modules}{\categoryname{Mod}}
243 \WithSuffix\newcommand\Modules*{\decoration{^*}{\textrm{-}}\Modules{}}

\LeftModules
244 \newcommand{\LeftModules}[1]{\textsf{-}\categoryname{Mod}{}}

\RightModules
245 \newcommand{\RightModules}[2]{\categoryname{Mod}_{}\#1\textsf{-}\#2\categoryname{Mod}{}}

\Bimodules
246 \newcommand{\Bimodules}{\categoryname{Bimod}}
247 \WithSuffix\newcommand\Bimodules*{\decoration{^*}{\textrm{-}}\Bimodules{}}

\Rings
248 \newcommand{\Rings}{\categoryname{Ring}{}}

\Groups
249 \newcommand{\Groups}{\categoryname{Group}{}}

\Ab
250 \newcommand{\Ab}{\categoryname{Ab}{}}

\Lattices
251 \newcommand{\Lattices}{\categoryname{Lattice}{}}

\Sets
252 \newcommand{\Sets}{\categoryname{Set}{}}

```

```

\Vect
253 \newcommand{\Vect}{\categoryname{Vect}}

\LieAlgs
254 \newcommand{\LieAlgs}{\categoryname{LieAlg}>

\Posets
255 \newcommand{\Posets}{\categoryname{Poset}>

\Directed
256 \newcommand{\Directed}{\categoryname{Directed}>

\GSets
257 \newcommand{\GSets}[1]{\text{\{}#1\text{\}}\text{\}\textit{Sets}>

\Groupoids
258 \newcommand{\Groupoids}{\categoryname{Groupoid}>

259 \fi

```

### 3.5 Analysis

First we check of macros should be included:

```
260 \if@loadmath
```

#### 3.5.1 General Analysis

```

\vol
261 \newcommand{\vol}{\mathrm{vol}>

\complete
262 \newcommand{\complete}[1]{\widehat{#1}>

\Ball
263 \newcommand{\Ball}{\mathrm{Ball}>

\abs
264 \DeclarePairedDelimiter{\abs}{\lvert}{\rvert}

\norm
265 \DeclarePairedDelimiter{\norm}{\lVert}{\rVert}

\supnorm
266 \newcommand{\supnormstar}[1]{\norm*{#1}_{\infty}}
267 \newcommand{\supnormnostar}[2]{\norm[#1]{#2}_{\infty}}
268 \newcommand{\supnorm}{\@ifstar\supnormstar\supnormnostar}

\expands
269 \newcommand{\expands}[1]{\mathrel{\scalebox{#1}[1.1]{\$sim\$}}}

```

### 3.5.2 Pseudodifferential Operators

```
\std  
270 \newcommand{\std}{{\scriptscriptstyle{\ch@irxscriptfont{std}}}}  
\Weyl  
271 \newcommand{\Weyl}{{\scriptscriptstyle{\ch@irxscriptfont{Weyl}}}}  
\Op  
272 \newcommand{\Op}{\operatorname{Op}}  
\Opstd  
273 \newcommand{\Opstd}{\operatorname{Op}_\std}  
\OpWeyl  
274 \newcommand{\OpWeyl}{\operatorname{Op}_\Weyl}
```

### 3.5.3 Function Spaces

```
\spacename  
275 \newcommand{\spacename}[1]{\ch@irxspacefont{#1}}  
\Bounded  
276 \newcommand{\Bounded}{\ch@irxspacefont{B}}  
\Continuous  
277 \newcommand{\Continuous}{\ch@irxspacefont{C}}  
\Contbound  
278 \newcommand{\Contbound}{\Continuous_{\mathrm{b}}}  
\Fun  
279 \newcommand{\Fun}[1][k]{\ch@irxspacefont{C}^{\#1}}  
\Cinfty  
280 \newcommand{\Cinfty}{\Fun[\infty]}  
\Comega  
281 \newcommand{\Comega}{\Fun[\omega]}  
\Holomorphic  
282 \newcommand{\Holomorphic}{\ch@irxspacefont{0}}  
\AntiHolomorphic  
283 \newcommand{\AntiHolomorphic}{\mathrm{cc}\{\Holomorphic\}}  
\Schwartz  
284 \newcommand{\Schwartz}{\ch@irxspacefont{S}}  
\Riemann  
285 \newcommand{\Riemann}{\ch@irxspacefont{R}}
```

### 3.5.4 Locally Convex Spaces

```
\singsupp  
286 \newcommand{\singsupp}{\operatorname{sing},\mathrm{supp}}  
  
\seminorm  
287 \newcommand{\seminorm}[1]{\mathrm{#1}}  
  
\ord  
288 \newcommand{\ord}{\operatorname{ord}}  
  
\conv  
289 \newcommand{\conv}{\operatorname{conv}}  
  
\extreme  
290 \newcommand{\extreme}{\operatorname{extreme}}
```

### 3.5.5 Hilbert Spaces

```
\hilbert  
291 \newcommand{\hilbert}[1]{\mathfrak{ch}@\mathrm{irxhilbertfont}{#1}}  
  
\prehilb  
292 \newcommand{\prehilb}[1]{\mathfrak{ch}@\mathrm{irxprehilbfont}{#1}}  
  
\Adjointable  
293 \newcommand{\Adjointable}[1][]{\mathfrak{B}_{\mathrm{\scriptscriptstyle{#1}}}}  
  
\Finite  
294 \newcommand{\Finite}[1][]{\mathfrak{F}_{\mathrm{\scriptscriptstyle{#1}}}}  
  
\Compact  
295 \newcommand{\Compact}[1][]{\mathfrak{K}_{\mathrm{\scriptscriptstyle{#1}}}}  
  
\opdomain  
296 \newcommand{\opdomain}{\mathfrak{ch}@\mathrm{irxhilbertfont}{D}}  
  
\spec  
297 \newcommand{\spec}{\operatorname{\mathfrak{ch}@\mathrm{irxoperatorfont}{spec}}}}  
  
\closure  
298 \newcommand{\closure}[1]{\overline{\mathrm{#1}}}  
  
\res  
299 \newcommand{\res}{\operatorname{\mathfrak{ch}@\mathrm{irxoperatorfont}{res}}}}  
  
\Res  
300 \newcommand{\Res}{\operatorname{\mathfrak{ch}@\mathrm{irxoperatorfont}{Res}}}}
```

```

\specrad
301 \newcommand{\specrad}{\operatorname{\varrho}}
\slim
302 \newcommand{\slim}{\operatorname{s-lim}}
\wlim
303 \newcommand{\wlim}{\operatorname{w-lim}}

```

### 3.5.6 Dirac's bra and ket

```

\bra
\ket 304 \DeclarePairedDelimiter{\ketbr@}{\langle}{\rangle}
\baket 305 \DeclarePairedDelimiter{\ket}{\langle}{\rangle}
\ketbra 306 \DeclarePairedDelimiter{\bra}{\langle}{\rangle}
307 \newcommand{\baket}[3]{\SP[\#1]{\#2}{\#3}\#1\langle\#3\rangle}
308 \newcommand{\ketbra}[3]{\ketbr@{\#1}{\#2}{\#1\langle\#3\rangle}}

```

### 3.5.7 Operator Algebras

```

\Spec
309 \newcommand{\Spec}{\operatorname{\mathfrak{S}pec}}
\Rad
310 \newcommand{\Rad}{\operatorname{\mathfrak{R}ad}}
\ind
311 \newcommand{\ind}{\operatorname{\mathfrak{ind}}}

```

### 3.5.8 Measure Theory and Integration

```

\Measurable
312 \newcommand{\Measurable}{\operatorname{\mathfrak{M}}}
\Meas
313 \newcommand{\Meas}{\operatorname{\mathfrak{Meas}}}
\BoundMeas
314 \newcommand{\BoundMeas}{\operatorname{\mathfrak{BM}}}
\mathbf{Lp}
315 \newcommand{\mathbf{Lp}}[1]{\mathrm{L}^{\#1}}
\mathbf{Lone}
316 \newcommand{\mathbf{Lone}}{\mathbf{Lp}[1]}
\mathbf{Ltwo}
317 \newcommand{\mathbf{Ltwo}}{\mathbf{Lp}[2]}

```

```

\Linfty
318 \newcommand{\Linfty}{\mathop{\mathrm{Lip}}[\infty]}

\Intp
319 \newcommand{\Intp}[1][p]{\mathop{\mathrm{chirxspacefont}}[L]^{\#1} }

\Intone
320 \newcommand{\Intone}{\Intp[1]}

\Inttwo
321 \newcommand{\Inttwo}{\Intp[2]}

\Intinfty
322 \newcommand{\Intinfty}{\Intp[\infty]}

\essrange
323 \newcommand{\essrange}{\operatorname{\mathop{\mathrm{chirxoperatorfont}}[ess],range}}}

\esssup
324 \newcommand*{\esssup}{\operatorname{\mathop{\mathrm{chirxoperatorfont}}[ess]},\mathop{\mathrm{chirxoperatorfont}}[\sup]}}

\essupnormstar
325 \newcommand{\essupnormstar}[1]{\mathop{\mathrm{norm}}^{\#1}_{\esssup}}
326 \newcommand{\essupnormstar}[2]{\mathop{\mathrm{norm}}^{\#1}_{\#2}_{\esssup}}
327 \newcommand{\essupnorm}{\mathop{\mathrm{essupnorm}}_{\mathop{\mathrm{ifstar}}[\essupnormstar]\essupnormstar} }

\ac
328 \newcommand{\ac}{\mathop{\mathrm{chirxscriptfont}}[ac]}

\sing
329 \newcommand{\sing}{\mathop{\mathrm{chirxscriptfont}}[sing]}

3.5.9 Limits

\indlim
330 \newcommand{\indlim}{\operatorname{\mathop{\mathrm{ind}},\mathrm{lim}}}

\projlim
331 \renewcommand{\projlim}{\operatorname{\mathop{\mathrm{proj}},\mathrm{lim}}}

332 \fi

```

## 3.6 Category Theory

First we check if macros should be included:

```
333 \if@loadmath
```

### 3.6.1 General Category Theory

General stuff for categories.

```
\category
334 \newcommand{\category}[1]{\ch@irxcategoryfont{#1}}


\categoryname
335 \newcommand{\categoryname}[1]{\ch@irxcategorynamefont{#1}}


\functor
336 \newcommand{\functor}[1]{\ch@irxfunctorfont{#1}}


\groupoid
337 \newcommand{\groupoid}[1]{\ch@irxgroupoidfont{#1}}


\source
338 \newcommand{\source}{\ch@irxoperatorfont{source}}


\target
339 \newcommand{\target}{\ch@irxoperatorfont{target}}


\unit
340 \newcommand{\unit}{\ch@irxoperatorfont{unit}}


\opp
341 \newcommand{\opp}{\ch@irxscriptfont{opp}}


\asso
342 \newcommand{\asso}{\ch@irxoperatorfont{asso}}


\Hom
343 \newcommand{\Hom}{\operatorname{\ch@irxoperatorfont{Hom}}{}}

\End
344 \newcommand{\End}{\operatorname{\ch@irxoperatorfont{End}}{}}



\Aut
345 \newcommand{\Aut}{\operatorname{\ch@irxoperatorfont{Aut}}{}}



346 \WithSuffix\newcommand{\Aut*}{\operatorname{\ch@irxoperatorfont{Aut}}{}^*}



\Iso
347 \newcommand{\Iso}{\operatorname{\ch@irxoperatorfont{Iso}}{}}



348 \WithSuffix\newcommand{\Iso*}{\operatorname{\ch@irxoperatorfont{Iso}}{}^*}



\Obj
349 \newcommand{\Obj}{\operatorname{\ch@irxoperatorfont{Obj}}{}}



\Morph
350 \newcommand{\Morph}{\operatorname{\ch@irxoperatorfont{Morph}}{}}


```

### 3.6.2 Colimits

```
\colim
351 \newcommand{\colim}{\operatorname*{{\{}{\colim}{\}}}}
352 \fi
```

## 3.7 Differential Geometry

First we check of macros should be included:

```
353 \if@loadmath
```

### 3.7.1 General Differential Geometry

```
\Lie
354 \newcommand{\Lie}{\mathscr{L}}
```

A generic bracket as paired delimiter, used in several other macros

```
\ch@irxbbracket
355 \DeclarePairedDelimiter{\ch@irxbbracket}{[]}{[]}
```

A generic double bracket as paired delimiter, used in several other macros

```
\ch@irxbbracket
356 \DeclareMathDelimiter{\ch@irxllbbracket}{\mathopen}{stmry}{4A}{stmry}{71}
357 \DeclareMathDelimiter{\ch@irxrrbbracket}{\mathclose}{stmry}{4B}{stmry}{79}
358 \DeclarePairedDelimiter{\ch@irxbbracket}{\ch@irxllbbracket}{\ch@irxrrbbracket}
```

```
\Schouten
359 \newcommand{\@schoutenstar}[1]{\ch@irxbbracket*{\#1}_{\scriptscriptstyle\ch@irxscriptfont{S}}}
360 \newcommand{\@schoutennostar}[2]{[\ch@irxbbracket{\#1}{\#2}_{\scriptscriptstyle\ch@irxscriptfont{S}}]}
361 \newcommand{\Schouten}{\@ifstar{\@schoutenstar}{\@schoutennostar}}
```

```
\Forms
362 \newcommand{\Forms}{\Omega}
```

```
\ZdR
363 \newcommand{\ZdR}{\ch@irxoperatorfont{Z}_{\scriptscriptstyle\mathsf{dR}}}
```

```
\BdR
364 \newcommand{\BdR}{\ch@irxoperatorfont{B}_{\scriptscriptstyle\mathsf{dR}}}
```

```
\HdR
365 \newcommand{\HdR}{\ch@irxoperatorfont{H}_{\scriptscriptstyle\mathsf{dR}}}
```

```
\Diffeo
366 \newcommand{\Diffeo}{\operatorname*{{\{}{\Diffeo}{\}}}}
```

```

\Diffop
367 \newcommand{\Diffop}{\operatorname{\ch@irxoperatorfont{DiffOp}}}

\loc
368 \newcommand{\loc}{\operatorname{\ch@irxscriptfont{loc}}}

\germ
369 \newcommand{\germ}{\operatorname{\ch@irxoperatorfont{germ}}}

\prol
370 \newcommand{\prol}{\operatorname{\ch@irxoperatorfont{prol}}}

\NRbracket
371 \newcommand{\@nrbracketstar}[1]{\operatorname{\ch@irxbracket*{#1}_{\scriptscriptstyle\ch@irxscriptfont{NR}}}}
372 \newcommand{\@nrbracketnostar}[2]{\operatorname{\ch@irxbracket[#1]{#2}_{\scriptscriptstyle\ch@irxscriptfont{NR}}}}
373 \newcommand{\NRbracket}{\@ifstar{\@nrbracketstar}{\@nrbracketnostar}{}}

\FNbracket
374 \newcommand{\@fnbracketstar}[1]{\operatorname{\ch@irxbracket*{#1}_{\scriptscriptstyle\ch@irxscriptfont{FN}}}}
375 \newcommand{\@fnbracketnostar}[2]{\operatorname{\ch@irxbracket[#1]{#2}_{\scriptscriptstyle\ch@irxscriptfont{FN}}}}
376 \newcommand{\FNbracket}{\@ifstar{\@fnbracketstar}{\@fnbracketnostar}{}}

\Manifold
377 \newcommand{\Manifolds}{\operatorname{\categoryname{\categoryname{Manifold}}}}

```

**3.7.2 Lie Groups and Principal Fiber Bundles**

```

\lefttriv
378 \newcommand{\lefttriv}{\operatorname{\ch@irxoperatorfont{left}}}

\righttriv
379 \newcommand{\righttriv}{\operatorname{\ch@irxoperatorfont{right}}}

\Gau
380 \newcommand{\Gau}{\operatorname{\ch@irxoperatorfont{Gau}}}

\Conn
381 \newcommand{\Conn}{\operatorname{\ch@irxoperatorfont{Conn}}}

\ratio
382 \newcommand{\ratio}{\operatorname{\ch@irxoperatorfont{r}}}

\Parallel
383 \newcommand{\Parallel}{\operatorname{\ch@irxoperatorfont{P}}}

\CE
384 \newcommand{\CE}{\operatorname{\scriptscriptstyle\ch@irxscriptfont{CE}}}

```

```

\HCE
385 \newcommand{\HCE}{\ch@irxoperatorfont{H}\_CE}

\fund
386 \newcommand{\fund}{\ch@irxoperatorfont{fund}}


\Universal
387 \newcommand{\Universal}{\operatorname{\ch@irxoperatorfont{U}}}

\BCH
388 \newcommand{\BCH}{\ch@irxscriptfont{\scriptscriptstyle{BCH}}}

\LieGroups
389 \newcommand{\LieGroups}{\categoryname{\categoryname{LieGroup}}}

\Principal
390 \newcommand{\Principal}{\categoryname{\categoryname{Principal}}}

\GPrincipal
391 \newcommand{\GPrincipal}[1][G]{\#1\categoryname{\textrm{-}}\categoryname{Principal}{}}

\Fiber
392 \newcommand{\Fiber}{\categoryname{Fiber}{}}

\FFiber
393 \newcommand{\FFiber}[1][F]{\#1\categoryname{\textrm{-}}\categoryname{Fiber}{}}

\Pin
394 \newcommand{\Pin}{\group{Pin}{}}

\Spin
395 \newcommand{\Spin}{\group{Spin}{}}

3.7.3 (Pseudo) Riemannian Geometry

\nablaLC
396 \newcommand{\nablaLC}{\nabla^{\scriptscriptstyle\ch@irxscriptfont{LC}}}

\Laplace
397 \newcommand{\Laplace}{\Delta}

\dAlembert
398 \DeclareMathSymbol\dAlembert{\mathord}{AMSA}{03}

\feynman
399 \newcommand{\feynman}[1]{\ooalign{\#1$\cr\hidewidth\raise0.19ex\hbox{/}\hidewidth\cr}}

```

```

\Dirac
400 \newcommand{\Dirac}{\feynman{D}}

\rotation
401 \newcommand{\rotation}{\operatorname{\ch@irxoperatorfont{rot}}}

\curl
402 \newcommand{\curl}{\operatorname{\ch@irxoperatorfont{curl}}}

\divergence
403 \newcommand{\divergence}{\operatorname{\ch@irxoperatorfont{div}}}

\gradient
404 \newcommand{\gradient}{\operatorname{\ch@irxoperatorfont{grad}}}

\Tor
405 \newcommand{\Tor}{\operatorname{\ch@irxoperatorfont{Tor}}}

\Ric
406 \newcommand{\Ric}{\operatorname{\ch@irxoperatorfont{Ric}}}

\scal
407 \newcommand{\scal}{\operatorname{\ch@irxoperatorfont{scal}}}

\Riem
408 \newcommand{\Riem}{\operatorname{\ch@irxoperatorfont{Riem}}}

\Hessian
409 \newcommand{\Hessian}{\operatorname{\ch@irxoperatorfont{Hessian}}}

\hodge
410 \newcommand{\hodge}{\operatorname{\star}}

```

### 3.7.4 Complex Geometry

```

\Nijenhuis
411 \newcommand{\Nijenhuis}{\operatorname{\ch@irxoperatorfont{Nij}}}

\del
412 \newcommand{\del}{\mathop{}!\partial}

\delbar
413 \newcommand{\delbar}{\mathop{}!\overline{\partial}^c}

\FS
414 \newcommand{\FS}{\operatorname{\scriptscriptstyle{\ch@irxscriptfont{FS}}}}

```

### 3.7.5 Vector Bundles

```

\Lift
415 \newcommand{\Lift}{{\scriptscriptstyle{\ch@irxscriptfont{Lift}}}}
```

```

\ver
416 \newcommand{\ver}{\ch@irxscriptfont{ver}}
```

```

\hor
417 \newcommand{\hor}{\ch@irxscriptfont{hor}}
```

```

\Ver
418 \newcommand{\Ver}{\operatorname{\ch@irxoperatorfont{Ver}}}
```

```

\Hor
419 \newcommand{\Hor}{\operatorname{\ch@irxoperatorfont{Hor}}}
```

```

\Sec
420 \newcommand{\Sec}[1][k]{\Gamma^{\#1}}
```

```

\Secinfy
421 \newcommand{\Secinfy}{\Sec[\infty]}
```

```

\HolSec
422 \newcommand{\HolSec}{\Sec[]_{\ch@irxscriptfont{hol}}}
```

```

\SymD
423 \newcommand{\SymD}{\mathop{}!\ch@irxoperatorfont{D}}
```

```

\Densities
424 \newcommand{\Densities}[1][n]{\abs{\Lambda^{\#1}}}
```

```

\MeasurableSections
425 \newcommand{\MeasurableSections}{\ch@irxspacefont{M}\Sec[]}
```

```

\IntpSections
426 \newcommand{\IntpSections}[1][p]{\Intp[\#1]\Sec[]}
```

```

\IntegrableSections
427 \newcommand{\IntegrableSections}{\IntpSections[1]}
```

```

\Translation
428 \newcommand{\Translation}{\ch@irxoperatorfont{T}}
```

```

\frames
429 \newcommand{\frames}[1]{\ch@irxoperatorfont{\#1}}
```

```

\Frames
430 \newcommand{\Frames}{\operatorname{\ch@irxoperatorfont{Frames}}}
```

```

\FDiff
431 \newcommand{\FDiff}{\ch@irxoperatorfont{F}}
```

### 3.7.6 Symplectic and Poisson Geometry

```

\Symp1
432 \newcommand{\Symp1}{\operatorname{\ch@irxgroupfont{Symp1}}}

\Jacobiator
433 \newcommand{\Jacobiator}[1][\pi]{\operatorname{\ch@irxoperatorfont{Jac}}_{\#1}{}}

\red
434 \newcommand{\red}{\operatorname{\ch@irxscriptfont{red}}}

\Hess
435 \newcommand{\Hess}{\operatorname{\ch@irxoperatorfont{Hess}}}

\KKS
436 \newcommand{\KKS}{\operatorname{\scriptscriptstyle\ch@irxscriptfont{KKS}}}

\Courant
437 \newcommand{\@courantstar}[1]{\operatorname{\ch@irxbbracket*{\#1}_{\scriptscriptstyle\ch@irxscriptfont{C}}}}
438 \newcommand{\@courantnostar}[2][]{\operatorname{\ch@irxbbracket[\#1]{\#2}_{\scriptscriptstyle\ch@irxscriptfont{C}}}}
439 \newcommand{\Courant}{\operatorname{\@ifstar{\@courantstar}{\@courantnostar}}}

\Dorfman
440 \newcommand{\@dorffmanstar}[1]{\operatorname{\ch@irxbbracket*{\#1}_{\scriptscriptstyle\ch@irxscriptfont{D}}}}
441 \newcommand{\@dorffmannostar}[2][]{\operatorname{\ch@irxbbracket[\#1]{\#2}_{\scriptscriptstyle\ch@irxscriptfont{D}}}}
442 \newcommand{\Dorfman}{\operatorname{\@ifstar{\@dorffmanstar}{\@dorffmannostar}}}

\Dir
443 \newcommand{\Dir}{\operatorname{\ch@irxoperatorfont{Dir}}}

\Forward
444 \newcommand{\Forward}{\operatorname{\mathcal{F}}}

\Backward
445 \newcommand{\Backward}{\operatorname{\mathcal{B}}}

\Tangent
446 \newcommand{\Tangent}{\operatorname{\mathbb{T}}}

\MWreduction
447 \newcommand{\MWreduction}{\big/\!\!\!/\!\!\!\big/}

\Mon
448 \newcommand{\Mon}{\operatorname{\ch@irxoperatorfont{Mon}}}

\Hol
449 \newcommand{\Hol}{\operatorname{\ch@irxoperatorfont{Hol}}}

450 \fi

```

## 3.8 Linear Algebra

First we check of macros should be included:

```
451 \if@loadmath
```

### 3.8.1 General Linear Algebra

```
\tr  
452 \newcommand{\tr}{\operatorname{\ch@irxoperatorfont{tr}}}  
  
\rank  
453 \newcommand{\rank}{\operatorname{\ch@irxoperatorfont{rank}}}  
  
\codim  
454 \newcommand{\codim}{\operatorname{\ch@irxoperatorfont{codim}}}  
  
\diag  
455 \newcommand{\diag}{\operatorname{\ch@irxoperatorfont{diag}}}  
  
\Trans  
456 \newcommand{\Trans}{\operatorname{\ch@irxscriptfont{\scriptscriptstyle{T}}}}  
  
\Mat  
457 \newcommand{\Mat}{\operatorname{\ch@irxoperatorfont{M}}}  
  
\SymMat  
458 \newcommand{\SymMat}{\operatorname{\ch@irxoperatorfont{SymMat}}}  
  
\ann  
459 \newcommand{\ann}{\operatorname{\ch@irxscriptfont{ann}}}  
  
\Span  
460 \newcommand{\Span}[1]{\operatorname{\ch@irxoperatorfont{span}_{#1}}}  
  
\basis  
461 \newcommand{\basis}[1]{\operatorname{\ch@irxbasisfont{#1}}}
```

### 3.8.2 Tensors

```
\tensor  
462 \renewcommand{\tensor}[1][{}]{\mathbin{\otimes_{\operatorname{\ch@irxscriptstyle{#1}}}}}  
  
\Tensor  
463 \newcommand{\Tensor}{\operatorname{\ch@irxoperatorfont{T}}}  
  
\Anti  
464 \newcommand{\Anti}{\Lambda}
```

```

\Sym
465 \newcommand{\Sym}{\ch@irxoperatorfont{S}}


\Symmetrizer
466 \newcommand{\Symmetrizer}{\operatorname{\ch@irxoperatorfont{Sym}}}

\AntiSymmetrizer
467 \newcommand{\AntiSymmetrizer}{\operatorname{\ch@irxoperatorfont{Alt}}}

\ins
468 \newcommand{\ins}{\operatorname{\ch@irxoperatorfont{i}}}

\jns
469 \newcommand{\jns}{\operatorname{\ch@irxoperatorfont{j}}}

\insa
470 \newcommand{\insa}{\operatorname{\ch@irxscriptfont{a}}}

\inss
471 \newcommand{\inss}{\operatorname{\ch@irxscriptfont{s}}}

\degs
472 \newcommand{\degs}{\operatorname{\ch@irxoperatorfont{deg}}_{\operatorname{\ch@irxscriptfont{s}}}}
```

### 3.8.3 Inner Products

### 3.9 Statistics

First we check if macros should be included:

478 \if@loadmath

### 3.9.1 General Statistics

```
\EX  
479 \newcommand{\EX}{\operatorname{\ch@irxoperatorfont{E}}}  
  
\Var  
480 \newcommand{\Var}{\operatorname{\ch@irxoperatorfont{Var}}}  
  
\Cov  
481 \newcommand{\Cov}{\operatorname{\ch@irxoperatorfont{Cov}}}  
  
\Cor  
482 \newcommand{\Cor}{\operatorname{\ch@irxoperatorfont{Cor}}}  
483 \fi
```

## 3.10 Topology

First we check of macros should be included:

```
484 \if@loadmath
```

### 3.10.1 General Topology

```
\cl  
485 \newcommand{\cl}{\operatorname{\ch@irxscriptfont{cl}}}  
  
\scl  
486 \newcommand{\scl}{\operatorname{\ch@irxscriptfont{scl}}}  
  
\interior  
487 \newcommand{\interior}{\circ}  
\boundary  
488 \newcommand{\boundary}{\partial}  
  
\supp  
489 \newcommand{\supp}{\operatorname{\ch@irxoperatorfont{supp}}}  
  
\dist  
490 \newcommand{\dist}{\operatorname{\ch@irxoperatorfont{dist}}}  
  
\topology  
491 \newcommand{\topology}[1]{\operatorname{\ch@irxtopologyfont{#1}}}  
  
\filter  
492 \newcommand{\filter}[1]{\operatorname{\ch@irxfilterfont{#1}}}
```

```

\sheaf
493 \newcommand{\sheaf}[1]{\ch@irxsheaffont{#1}}


\Sections
494 \newcommand{\Sections}{\operatorname{\ch@irxoperatorfont{Sections}}}

\HOM
495 \newcommand{\HOM}{\operatorname{\ch@irxsheaffont{H}\! \mathit{om}}}

\etale
496 \DeclarePairedDelimiter{\etale}{\lvert}{\rvert}

```

**3.10.2 Categories from Topology**

```

\topological
497 \newcommand{\topological}{\categoryname{top}}


\Topological
498 \newcommand{\Topological}{\categoryname{Top}}


\Sheaves
499 \newcommand{\Sheaves}{\categoryname{Sheaves}}


\PreSheaves
500 \newcommand{\PreSheaves}{\categoryname{PreSheaves}}


\Etale
501 \newcommand{\Etale}{\categoryname{Etale}}


502 \fi

```